# Partner Synthesis for Data-Dependent Services

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**Abstract.** A service is *controllable*, if there exists a service with which it can interact properly. We sketch an approach to decide controllability for a certain class of services. Controllability is decided by synthesizing a service that controls the given service. For a class of services which abstracts from data, the synthesis problem is already solved. In this paper, we present an approach for a class of services that deals with data explicitly.

## 1 Introduction

A service is designed with the goal that it can interact with another service. A service may interact properly with one service but not interact properly with an other service. For example, two services may end up blocking each other, making any further interaction impossible. The possibility of the occurrence of an error depends on both interacting services and in general can not be attributed to one service alone. However, at the time of design of a service, the other services the service will be interacting with typically are not known in advance. Nevertheless, we can check a fundamental property called *controllability* [7] when considering one service in isolation. A service is called *controllability* can be decided by *synthesizing* a service that interacts with the given service properly.

The synthesis problem is solved for the finite automaton based service model used in [3,7]. This service model abstracts from data, i. e. messages are not distinguished by their content. For a more realistic model which takes data into account, the synthesis problem is still open. The goal of our work is to solve the synthesis problem for a service model that includes data.

In Sect. 2, we introduce the concept of a *partner* of a service. Section 3 presents an approach to synthesize a partner for a High-Level Petri net based service model. Section 4 concludes our work.

### 2 Partners

We represent a service by an *open net* [3] (Fig. 1). An open net is a Petri net with distinguished *interface places* that represent channels for asynchronous message exchange. We use High-Level Petri nets [2] so that data can be represented by coloured *tokens*.

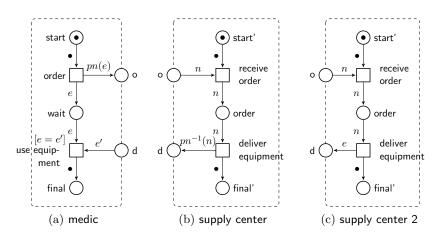


Fig. 1: Some open nets

The following example illustrates the interaction of a medic with a medical supply center from which the medic orders medical equipment. Both the medic and the supply center are services represented by the open nets in Fig. 1a and Fig. 1b. The composition (medic $\oplus$ supply center) of the open nets medic and supply center is the Petri net we obtain by fusing the interface places o and d. The medic orders medical equipment by *firing* the transition order. Thereby the token • is removed from place start. The variable *e* is assigned the equipment the medic orders, e. g., a syringe. Therefore, a token with value syringe is produced on place wait. The term pn(e) evaluates to the product number of the syringe. A token with that value is produced on the output place o. This corresponds to sending a message to supply center.

The medic waits for an incoming delivery on place d. supply center receives the order message from o by firing receive order and n is assigned the product number of syringe. The transition deliver equipment takes the product number from place order and produces the equipment corresponding to that number (in this case syringe) on interface place d. Since the tokens on wait and d are equal, the guard e = e' of transition use equipment is fulfilled. Therefore use equipment can fire and (medic $\oplus$ supply center) reaches its final marking, i. e. the marking in which both places final and final' are marked with the token  $\bullet$ .

Two open nets  $N_1$  and  $N_2$  are called *partners*, if from each reachable marking of  $N_1 \oplus N_2$  a final marking of  $N_1 \oplus N_2$  is reachable. The medic and supply center are partners. The medic and supply center 2 are not partners: When deliver equipment fires, any arbitrary equipment may be assigned to e which in general does not correspond to the product number assigned to n. Therefore, there is a marking reachable in (medic $\oplus$ supply center) with a token with value syringe on wait and a token with another value (e. g. stethoscope) on d. This marking is a *deadlock*, because e = e' is not satisfied and use equipment can not fire. On acyclic open nets, the reachability of a final marking is equivalent to deadlock freedom. An open net  $N_1$  is called *controllable*, if it has a least one partner. medic is controllable. In this example, we assumed that function pn has an inverse  $pn^{-1}$ . However, if we replace pn by a function pn' which is not bijective, medic becomes uncontrollable. In that case, a supply center can not infer the equipment the medic is waiting for from the product number. Therefore, it is not possible to guarantee that e = e' is always satisfied and the final marking will be reached.

In the next section, we sketch an approach to synthesize a partner for a specific class of open nets.

## 3 Partner Synthesis

In this section, we sketch a partner synthesis algorithm for a given open net N. We consider a class of Petri nets where the domain of the variables and the colours of the tokens is infinitely large. The guards are denoted in a subset of first order logic that contains boolean algebra and quantifiers. For computational reasons, we assume that this subset is decidable (like e. g. Presbuger arithmetic [5]). We also assume that N is acyclic and the number of tokens on each place is at most one. Therefore, the length of each path in the state space of N is bounded by some number k.

Due to infinitely many colours, the state space of N is infinitely large. Therefore the synthesis algorithm for finite state services given in [7] can not be applied to our service model. Nevertheless, conceptually, our synthesis algorithm follows a similar approach. Therefore, we briefly outline the approach used for finite state services: First, an *over-approximation* of the partner of N that will be synthesized, i. e., a service that is guaranteed to contain a partner as a subgraph, is generated. Then certain states are removed from the over-approximation iteratively. The iteration is repeated as long as the composition of the given service and the over-approximation contains a deadlock. Eventually, two cases may occur: 1. The composition is deadlock-free. Then the remaining sub-graph of the over-approximation is a partner. 2. Every state has been removed. Then N is not controllable.

Now we give an overview of our synthesis algorithm. The details will be explained later by example. First, we construct an over-approximation  $S_0$  of the partners of N.  $S_0$  is a prefix of depth k of an infinite tree-like open net U we call universal environment. Then we iteratively add guards to  $S_0$ . Adding a guard corresponds to removing states from the over-approximation in the finite case. The iteration is repeated until no deadlock is reachable in the composition of Nand  $S_0$ . Each time a guard is added, some of the deadlocks of the composition become unreachable. Each iteration step may also introduce new deadlocks which will then be eliminated in the next iteration step. If (and only if) N is controllable, the composition will eventually be deadlock free and the modified  $S_0$  is a partner.

Now we show the derivation of a partner of medic from Fig. 1a. We assume that the colours of medic are integers and pn is the bijective function with pn(x) = x + 1. Therefore, medic can be expressed with Presburger arithmetic.

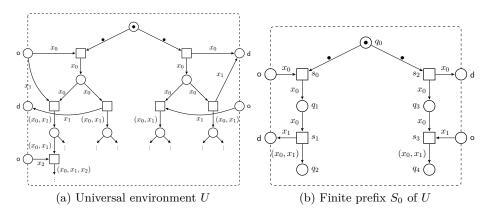


Fig. 2: Universal environment and its prefix. Interface places **o** and **d** are depicted multiple times to improve readability.

Fig. 2a shows the universal environment of medic. U is an infinite open net that has the inverse interface of N. U has a regular tree-like structure and can send and receive any (possibly infinite) sequence of messages. Therefore, U is an over-approximation of every partner of N. U stores every message sent or received from N. Each of the variables  $x_0, x_1, \ldots$  corresponds to the value of a message. These variables will be used in the guards which we will add later on. Since U is infinitely large, it is not suited for computational methods. Due to the acyclicity of N, the number of messages N can send and receive is bounded by a number k. Therefore, the prefix of U of depth k is still an over-approximation of the partners of N.

In the example, k is 2. In this particular case, we can even remove the branches of U which send or receive two messages on the same interface place without destroying the over-approximation property. This is possible because **medic** sends or receives at most one message on each interface place. Thus, we get the prefix  $S_0$  of U in Fig. 2b.

Now we iteratively derive a guard for each transition of  $S_0$ . The transitions are processed in bottom-up order. Thereby, we obtain a sequence  $S_0, S_1, S_2, \ldots$  of open nets with successively smaller reachability graphs.

Intuitively, a guard forbids a transition s of  $S_0$  to fire in a certain firing mode if there is the possibility to reach a deadlock after s has fired in that mode. That way, deadlocks are successively removed from the composition.

Since a transition has infinitely many firing modes, we need a syntactical representation of all firing modes that may not lead to a deadlock. We derive the guard predicate that is assigned to each transition using a technique outlined in [6]. The technique is based on the symbolic reachability graph (SRG) of a High-Level Petri net. The symbolic reachability graph is a compact representation of the reachability graph that allows to represent a possibly infinite set of markings by a symbolic marking. Fig. 3 shows the SRG of the composition medic  $\oplus S_0$ . In a symbolic marking M, every value is represented by a term. Attached to M is a

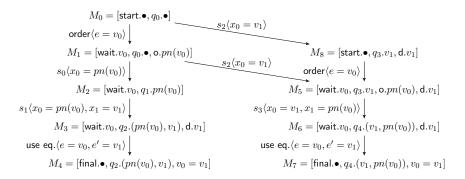


Fig. 3: Symbolic reachability graph of  $\mathsf{medic} \oplus S_0$ 

condition COND(M) which restricts the set of valid assignments to the variables that occur in M. A marking m is reachable if and only if there is a symbolic marking M that evaluates to m for an assignment that satisfies COND(M). Technically, during the construction of the SRG, COND(M) is formed by the conjunction of the effects of every guard on a path to M. Each edge of the SRG is inscribed by a transition t and a symbolic firing mode. A symbolic firing mode of t assigns a term to each variable of t.

In our example, the integer that is chosen non-deterministically by order for e is represented by the variable  $v_0$  in marking  $M_1$ . Analogously, the integer sent by  $s_1$  on d is represented by  $v_1$ . The effect of the guard e = e' of use equipment is represented by the condition  $v_0 = v_1$  of the markings  $M_4$  and  $M_7$ . Every other symbolic marking has the condition true.

The method we use to derive the guard of a transition s of  $S_0$  is inspired by Dijkstra's predicate transformer semantics [1]. The guard predicate can be regarded as the *weakest pre-condition* so that after firing of the transition s a specific post-condition holds. Here, the post-condition describes the assignments for which no subsequent symbolic marking evaluates to a deadlock. For each symbolic marking M we define a predicate DF(M) that describes for which assignments of the variables  $v_0, v_1, \ldots$  of the SRG M does not evaluate to a deadlock. DF(M) is formed by the disjunction of the conditions of the successors of M. The SRG and the DF predicates are recalculated in each iteration step. We denote the iteration step by a subscript.

 $M_4$  and  $M_7$  are final markings. Therefore,  $DF_0(M_4) \equiv DF_0(M_7) \equiv true$ . Since  $M_3$  has a successor marking only for those assignments of  $v_0$  and  $v_1$  with  $v_0 = v_1$ , we get  $DF_0(M_3) \equiv v_0 = v_1$ . Analogously,  $DF_0(M_6) \equiv v_0 = v_1$ . For every other symbolic marking M we get  $DF_0(M) \equiv true$ .

From every predicate DF(M), we derive a predicate DF'(M) which expresses the condition that M does not evaluate to a deadlock in terms of the variables used by the transition s of  $S_0$  that precedes M in the SRG (s is unique because  $S_0$ is a tree). By assigning DF(M) as a guard to s, every evaluation of M which is a deadlock becomes unreachable. The relationship between the variables  $x_0, x_1, \ldots$  of  $S_0$  and the variables  $v_0, v_1, \ldots$  of the SRG is established by the the symbolic firing mode of s.

In the example,  $M_3$  is reachable via exactly one path of the SRG. The last transition of  $S_0$  on this path is  $s_1$  with the symbolic firing mode  $\langle x_0 = pn(v_0), x_1 = v_1 \rangle$ . As stated above,  $DF_0(M_3) \equiv v_0 = v_1$ . With  $x_0 = pn(v_0), x_1 = v_1$  and the assumption that pn is injective follows that  $v_0 = v_1$  is equivalent to  $pn^{-1}(x_0) = x_1$ . Formally, we express this transformation by universal quantification of  $v_0, v_1$ :

$$DF'_0(M_3) \equiv \forall v_0, v_1 : x_0 = pn(v_0) \land x_1 = v_1 \implies v_0 = v_1$$
$$\equiv x_1 = pn^{-1}(x_0)$$

In words:  $DF'_0(M_3)$  describes all assignments of  $x_0, x_1$  for which the post-condition  $v_0 = v_1$  is guaranteed to hold after the firing of  $s_1$  in mode  $\langle x_0 = pn(v_0), x_1 = v_1 \rangle$ , regardless of which integers might have been non-deterministically chosen for  $v_0, v_1$ .

The general form of a DF' predicate (for the special case that there is only one path in the SRG to M) is

$$\forall v_0, \dots, v_j : COND(M) \land x_0 = T_0 \land \dots \land x_n = T_n \implies DF(M)$$

where  $\langle x_0 = T_0, \ldots, x_n = T_n \rangle$  is the symbolic firing mode of the last transition s of  $S_0$  on the path to M.

For  $M_4$ , we obtain  $DF'(M_4) \equiv true$ . We add the conjunction  $DF'(M_3) \wedge DF'(M_4)$  as a guard to the transition  $s_1$  that precedes both  $M_3$  and  $M_4$  in the SRG. After adding this guard  $x_1 = pn^{-1}(x_0)$  to  $s_1$ , every deadlock in which  $q_2$  is marked becomes unreachable.

We repeat this procedure for  $s_3$ .  $M_6$  is reachable via two paths of the SRG (which differ only insignificantly). The last transition of  $S_0$  on both paths is  $s_3$  with firing mode  $\langle x_0 = v_1, x_1 = pn(v_0) \rangle$ . Analogously, we get

$$DF'_0(M_6) \equiv \forall v_0, v_1 : x_0 = v_1 \land x_1 = pn(v_0) \implies v_0 = v_1$$
$$\equiv x_1 = pn(x_0)$$

In a more general case, we may get a different predicate for each path on which a marking M is reachable. Then DF'(M) is the conjunction of these predicates. With  $DF'_0(M_7) \equiv true$  we get the conjunction  $DF'_0(M_6) \wedge DF'_0(M_7) \equiv x_1 = pn(x_0)$ . After assigning  $x_1 = pn(x_0)$  to  $s_3$  as a guard, no deadlock is reachable in which  $q_4$  is marked.

Let  $S_1$  be the open net derived from  $S_0$  by adding the two guards to  $s_1$  and  $s_3$ . These guards introduce new deadlocks in which  $q_2$  and  $q_4$  are not marked, e. g. [wait.0,  $q_3.3$ , o.1, d.3] is a deadlock in medic  $\oplus S_1$  but not a deadlock of medic  $\oplus S_0$ . These new deadlocks will become unreachable in the next iteration step. In the SRG of medic  $\oplus S_1$  (Fig. 4),  $M_3$  has the condition  $v_0 = v_1$  and  $M_6$  has the condition  $pn(v_0) = pn(v_1)$  due to the guards that were added. Therefore we obtain the predicates

$$DF'_1(M_2) \equiv \forall v_0 : x_0 = pn(v_0) \implies \exists v_1 : v_0 = v_1 \equiv true$$
$$DF'_1(M_5) \equiv \forall v_0, v_1 : x_0 = v_1 \implies pn(v_0) = pn(v_1) \equiv false$$

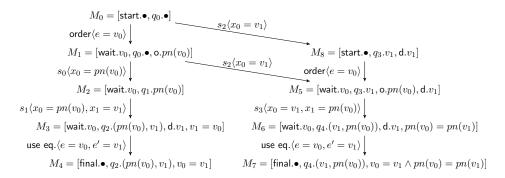


Fig. 4: Symbolic reachability graph of  $\mathsf{medic} \oplus S_1$ .

Variable  $v_1$  is existentially quantified, because  $v_1$  is not yet defined in  $M_2$  but will be created and chosen appropriately by  $s_1$  in the step from  $M_2$  to  $M_3$ . Please note that existential quantifiers may only appear as a part of a DF' predicate.

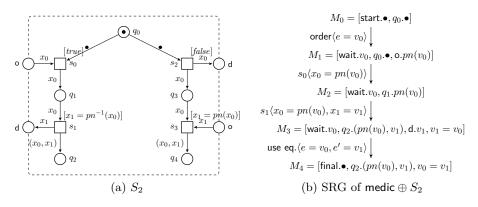


Fig. 5: Last iteration step of the partner synthesis

Eventually, by assigning the predicate  $DF'_1(M_2) \equiv true$  to  $s_0$  and  $DF'_1(M_5) \equiv false$  to  $s_2$ , we obtain the open net  $S_2$  shown in Fig. 5a. By repeating our calculation on the SRG of medic  $\oplus S_2$  (Fig.5b), we obtain  $DF_2(M_0) \equiv true$ . This indicates that no reachable marking in which  $q_0$  is marked is a deadlock. Therefore, every deadlock has been eliminated from medic  $\oplus S_2$  and  $S_2$  is a partner of medic by definition. Please note that  $S_2$  is very similar to  $N_2$  from Fig. 1b. In general, the last open net  $S_i$  of the sequence is a partner of N iff for every symbolic marking M in which the root place  $q_0$  is marked the predicate  $DF_i(M)$  is fulfilled for every assignment that fulfils  $COND_i(M)$ .

#### 4 Conclusion

We sketched an algorithm to synthesize a partner of a service represented by a High-Level Petri net. Currently, our approach is limited to acyclic services. We show a systematic approach to derive the relations between the values of incoming and outgoing messages that a service has to adhere to in order to be a partner of the given service. Since relations are denoted in first-order logic which is undecidable in the general case, we rely on an oracle to decide controllability. For a decidable theory like presburger arithmetic [5], controllability can be effectively computed. The technical details of the approach are not yet fully worked out.

Lohmann et al. [4] sketch a different approach to synthesize a partner for a High-Level Petri net based service. They use a symbolic representation for markings similar to ours. Their work focuses on the construction of the structure of the partner and only briefly discusses the derivation of the predicates. They give an ad-hoc explanation of the construction of the predicates for a particular example but do not describe a general derivation method. In particular, values that are non-deterministically chosen by the service are not treated.

In contrast to their approach, our approach does not consider structural aspects of the partner synthesis at all. All information concerning the behaviour of the partner is encoded by the guards. The structure of the partner is chosen in a generic way. However, our approach can handle values that are nondeterministically chosen by the service.

In our future work we aim at extending our approach to cyclic services. In this scenario it may be advantageous to chose a specific structure for the synthesized partner. E. g. case distinctions for specific values should result in a distinct node for each case. With a structure reflecting the behaviour of the service, it will be easier to identify isomorphic branches of the structure and nodes that can be combined without changing the behaviour. In order to ensure termination of the synthesis algorithm in the cyclic case, it is necessary to guarantee that there will be only finitely many nodes after the nodes have been combined.

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