USING GIS DATA TO IDENTIFY LINEAR OBSERVATION MODEL ON REMOTE SENSING IMAGES IN CASE OF SPATIAL MISMATCH OF INPUT IMAGE AND VECTOR MAP

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Abstract. This paper presents an experimental research of identification method proposed by the authors in their previous works. The method was developed to identify a linear observation model in remote sensing images. It uses the relation between energy spectra of input and output images, and it is called energy spectrum method. The latest modification of the method applies vector map data from geoinformation system to construct an image with energy spectrum similar to energy spectrum of unknown undistorted image. Vector map and input image had been supposed to be exactly spatially coherent. In this paper the algorithm’s quality is investigated in case of inexact spatial matching of input image and vector map. Accuracy of input image georeference and accuracy of vector map borders are considered as major spatial mismatch factors. Experimental evaluation of the these factors influence on quality of impulse response restoration is provided.

Keywords: identification of linear observation model, impulse response, energy spectrum method, geoinformation systems, vector map, georeferencing.

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1 Introduction

The common way to describe the process of image acquisition in remote sensing systems is a linear observation model [1]. For different applications, for example, for image correction, it is important to estimate the parameters of the model using only observed image. State of the art methods of system’s impulse response identification [2-4] work mainly with one dimensional signals or have high computational complexity, that significantly impedes their use in case of remote sensing images.
In papers [5-6] we described an approach of system impulse response estimation based on the relation between energy spectra of observed image and original undistorted image. It is called energy spectrum method. It supposes that original image is unknown. The method allows to identify two dimensional symmetrical nonnegative impulse response.

Occurrence of geoinformation systems (GIS) and electronic map services makes possible to use accumulated vector data for remote sensing image processing. In article [7] we proposed a modification of energy spectrum method using GIS data. This modification was considered in case of exact geometrical matching of observed image and vector map. In practice this condition may not be satisfied because of georeferencing errors and borders changes caused by lower updating rates for vector data.

The aim of present research is to evaluate experimentally an influence of spatial mismatch factors on the quality of impulse response estimation. The paper is organized as follows. In first section we adduce the computer realization of energy spectrum method using GIS data. The second section describes experimental research of the method in case of inexact georeferencing of observed image and mismatch of object borders on observed image and vector map.

2 Energy spectrum method modification using GIS data

Let us suppose that observed discrete image \( y_d(n_1, n_2) \) has sampling step \( T \) and size \( N \times N \), where \( n_1, n_2 = 0, N - 1 \) are integer pixel coordinates, and unknown original image \( x(m_1, m_2) \), \( m_1, m_2 = 0, M - 1 \) is also discrete with sampling step \( T_1 < T \). To simplify further descriptions it is assumed that \( M \) and \( N \) are even numbers and the ratio of sampling steps is denoted as \( \gamma = T / T_1 \).

If the noise dispersion \( D_\gamma \) is already evaluated, the energy spectrum method using GIS data for estimation of unknown impulse response \( h(k_1, k_2), k_1, k_2 = -K, K \) can be written as follows:

1. Build raster mask \( D(m_1, m_2), m_1, m_2 = 0, M - 1 \) of object borders from the vector map with sampling step \( T_1 \). Each object \( D_i \) corresponds to pixels with value \( i, i = 1, I \), where \( I \) is amount of objects on the image.
2. Interpolate observed image \( y_d(n_1, n_2) \) with step \( 1 / \gamma \) and size \( M \times M \). Received image is denoted as \( y_{in}(m_1, m_2) \), \( m_1, m_2 = 0, M - 1 \).
3. Make piecewise-constant image with sharp borders \( x(m_1, m_2), m_1, m_2 = 0, ..., M - 1 \) by means of averaging pixels for each object \( x(m_1, m_2) = y_i, m_1, m_2 \in D_i, i = 1, I \),

\[
y_i = \frac{1}{|D_i|} \sum_{m_1, m_2 \in D_i} y_{in}(m_1, m_2),
\]

(1)
where $|D_i|$ is the number of pixels for object with index $i$.

4. Calculate an estimation of unknown original image energy spectrum $\Phi_X(l_1,l_2)$.

$$l_1,l_2 = -\frac{M}{2}, \ldots, \frac{M}{2} - 1$$

using $x(m_1,m_2)$, $m_1, m_2 = 0, \ldots, M - 1$ by means of discrete Fourier transform with length $M$. Pixels with indexes $l_1, l_2 = -\frac{M}{2}, \ldots, \frac{M}{2} - 1$ correspond to frequencies $\Omega_1 = \frac{2\pi l_1}{M}, \Omega_2 = \frac{2\pi l_2}{M}$.

5. Calculate energy spectrum $\Phi_Y(l_1,l_2)$ of observed image $y_x(n_1,n_2)$, $n_1, n_2 = 0, \ldots, N - 1$ using discrete Fourier transform with length $N$. Pixels with indexes $p_1, p_2 = -\frac{N}{2}, \ldots, \frac{N}{2} - 1$ corresponds to frequencies $\Omega_1 = \frac{2\pi p_1}{N}, \Omega_2 = \frac{2\pi p_2}{N}$.

6. Calculate energy spectrum $\Phi_Y(l_1,l_2)$ by adding zeros to spectrum $\Phi_Y^{(d)}(p_1, p_2)$:

$$\Phi_Y(l_1,l_2) = \begin{cases} \gamma^2 \Phi_Y^{(d)}(l_1,l_2) - D_q, \\ npu - \frac{N}{2} \leq l_1 < \frac{N}{2} u - \frac{N}{2} \leq l_2 < \frac{N}{2}; \\ 0, \\ npu - \frac{M}{2} \leq l_1 < -\frac{N}{2} u - \frac{M}{2} \leq l_2 < \frac{M}{2}, \\ \frac{N}{2} \leq l_1 < \frac{M}{2} u - \frac{M}{2} \leq l_2 < \frac{M}{2}, \\ -\frac{N}{2} \leq l_1 < \frac{N}{2} u - \frac{M}{2} \leq l_2 < \frac{M}{2}, \\ -\frac{N}{2} \leq l_1 < \frac{N}{2} u \frac{N}{2} \leq l_2 < \frac{M}{2}. \end{cases}$$

7. Achieve an estimation of frequency response $H(l_1,l_2)$, $l_1, l_2 = -\frac{M}{2}, \ldots, \frac{M}{2} - 1$:

$$H(l_1,l_2) = \frac{\Phi_Y(l_1,l_2)}{\Phi_X(l_1,l_2)}$$

8. Find impulse response $\hat{h}(k_1, k_2)$ using discrete Fourier transform with length $M$.

Optional pixels with $|k_1, k_2| \geq K$ can be set to zero.

An estimations of energy spectrum on stages 4 and 5 could be obtained using standard methods of digital spectral analysis. To know more about these methods see [7].
3 Experimental research

Preparation of input data for the experiments includes following stages:

1. Generate original undistorted image and borders mask corresponding to it. Both images have sampling step $T_1$ and size $M \times M$ pixels. Correlation coefficient between neighbor pixels of original undistorted image is denoted as $\rho$.

2. Incorporate distortions into image by means of convolution of original image with given impulse response having sampling step $T_1$. This impulse response was used as etalon.

3. Digitize distorted image with size $M \times M$ in $\gamma$ times. Resulting image had size $N \times N$ pixels and sampling step $T$. It was interpreted as observed image with accurate geometrical parameters.

4. The last stage is including spatial mismatch to observed image and objects border mask.

In all experiments sampling steps and impulse responses were defined according to chosen sensor model. In this study we present results for

- MODIS sensor (Terra\Aqua) [1] with parameters $T_1 = 31.25$ m, $T = 250$ m and impulse response: $h_M(k_1, k_2) = h_i(k_1, k_2)^{**}h_2(k_1, k_2)^{**}h_3(k_1, k_2)$.

- ETM+ sensor (Landsat-7) [1] with parameters $T_1 = 3.75$ m, $T = 30$ m and impulse response: $h_U(k_1, k_2) = h_i(k_1, k_2)^{**}h_2(k_1, k_2)$,

where ** is convolution, $h_i(k_1, k_2) = A\exp\left[-0.5(k_1^2 + k_2^2)/\sigma^2\right]$ models smoothing of image due to defocusing; $h_2(k_1, k_2) = \text{rect}(k_1/w)\text{rect}(k_2/w)$ is impulse response of detector; $h_3(k_1, k_2) = \text{rect}(k_1/s)$ corresponds to motion-blur, $k_1, k_2 = -K, K$. In the first case parameters of impulse response were $\sigma = 123.5$ m [10], $w = s = 250$ m [1] and $K = 20$, in the second case they were $\sigma = 30$ m, $w = 30$ m [9], $K = 30$.

Quality of impulse response restoration was evaluated as root mean square error (RMSE) normalized by maximum (central) value of ideal impulse response:

$$
\varepsilon = \frac{1}{(2K+1)h(0,0)} \left[ \sum_{k_1,k_2 = -K}^{K} \left( h(k_1, k_2) - \hat{h}(k_1, k_2) \right)^2 \right], \quad (4)
$$

where $h(k_1, k_2)$ is ideal impulse response, $\hat{h}(k_1, k_2)$ is estimated impulse response. Expression (4) can be interpreted as relative error of impulse response restoration. The experimental research was made with absence of noise.
3.1 Quality of impulse response restoration in case of inexact georeference of input image

To investigate the influence of georeference accuracy on the quality of impulse response estimation mosaic images were used as input. Input images were generated in accordance with the process described above with following parameters $M = 4096$, $\rho = 0.99$, $N = 512$. The example of observed picture is shown in fig. 1.

![Image](image.png)

Fig. 1. The example of observed image

On the fourth stage observed images were shifted horizontally (diagonally) relatively to initial position by $B = 1,...,5$ pixels of observed image. Experimental results are shown in fig. 2.

![Graph](graph.png)

Fig. 2. Impulse response restoration RMSE depending on shift parameter $B$ for different sensor models: a) MODIS, b) ETM+
It is seen from the charts that average value of impulse response estimation error does not exceed 10% in case of MODIS sensor model and shift parameter value about 2-3 pixels of observed image. Such georeference accuracy meets the requirements of many image processing methods and can be achieved by standard georeferencing methods.

As for the impulse response modeling ETM+ sensor, shifting becomes a problem and does not allow to reconstruct it with appropriate accuracy. The reason is wider impulse response with higher smoothing characteristics in terms of observed image pixels.

3.2 Quality of impulse response restoration in case of objects borders mismatch on vector map and observed image

In order to estimate the influence of inexact vector map on the quality of impulse response restoration, simulated images were used. The images of agricultural landscape from Landsat 7 were transformed into piecewise-constant form by averaging pixel values within the borders of agricultural fields vector map for the same sowing season. Piecewise-constant images represented original undistorted image data and had following parameters $M = 2048$, $\rho = 0.95$, $N = 256$. Ideal border mask was made as a result of initial vector map rasterization. Distortions in vector map were made as a result of partial replacement of objects’ borders by borders from previous sowing season of the same objects. We used the following ratio: $\Delta S = \bar{S}/\bar{S}$ As quantitative characteristic of borders mismatch, where $\bar{S}$ is an area of disagreement of ideal and distorted border masks, and $\bar{S}$ is total area of objects on ideal mask. Both values $S$ and $\bar{S}$ are measured in pixels of original undistorted image. The example of observed image and binary image of mismatched vector regions are presented in fig. 3. The value of $\Delta S$, corresponding to the example on fig. 3, equals to 0,025.

![Fig. 3. Examples of: a) observed image and b) binary image of mismatched vector regions (black color - changes in vector mask)](image)
In fig. 4 the graph of impulse response RMSE depending on $\Delta S$ value is presented. It can be seen that border changes up to 2% of total objects area do not affect on quality of restoration.

![Graph of impulse response RMSE](image.png)

*Fig. 4. Impulse response restoration RMSE depending on mask border changes area*

However, RMSE is significantly higher than in previous experiment. The reason is that mosaic images had simpler borders geometry than the real vector map objects. The influence of borders geometry on quality of impulse response restoration is the question of future research.

**Conclusion**

The experimental research presented in paper shows that energy spectrum method using GIS data can be applied in case of inexact spatial matching of observed image and vector map. It was shown that allowable georeferencing error is about 2 or 3 pixels of observed image as a result of simulation for MODIS impulse response. Experiments also shown that allowable changes in borders of vector map are about 2% from total area of objects.

Further research deals with estimation border geometry influences on the quality of impulse response restoration and with developing of method’s modification that will be stable to various spatial mismatches in vector map and image data.

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