# A Hybrid Method of Information Aggregation for Community-level Decision-making

Sergii Kadenko 1[0000-0001-7191-5636]

<sup>1</sup> Institute for Information Recording of the National Academy of Sciences of Ukraine, Kyiv, Ukraine seriga2009@gmail.com

Abstract. When it comes to community-level decision making it is appropriate to utilize expert data based-methods, as the respective subject domains are, mostly, weakly structured ones. At the same time, during decision-making, opinion of the target territorial community members should be taken into consideration alongside expert data. The paper outlines an original method for formal description of weakly structured community-level problems, which uses both expert information and opinion of respondents from among community members. It represents a hybrid approach, incorporating elements of both traditional expert data-based methods and social surveys (questionnaires). The main goal (problem) is formulated by a decision-maker or research organizer. It is then decomposed by experts into sub-goals or factors that are crucial for its achievement, and these factors and their weights are estimated by respondents who are ordinary community members. The method includes the following conceptual steps: hierarchical decomposition of the problem, direct estimation of importance of factors that influence the problem, estimation of lowest-level "non-decomposable" factors by respondents in Likert agreement scale, and rating of the factors based on respondents' estimates through linear convolution (weighted summing). The obtained ratings provide the basis for defining toppriority activities that should be performed in order to solve the problem, and for subsequent distribution of limited resources among these activities. Experimental results, obtained in the process of actual research of public space quality, illustrate the method's application, and confirm its high efficiency. The advantages of the suggested method are efficiency and, at the same time, ease of use. In contrast to traditional expert data-based methods, it does not require any preliminary coaching sessions to be held with the respondents. The method is intended for decision-making support at the level of territorial communities (urban, rural, district, neighborhood, and others) in the spheres, directly related to the interests of community members. Target users of the method include local self-government bodies, media, public and volunteer organizations, activists, and other interested parties ...

**Keywords:** information aggregation, decision-making support, weakly structured subject domain, expert estimate, hierarchic problem decomposition, Likert agreement scale.

# 1 Introduction: Problem Relevance and Existing Approaches

Weakly structured nature is inherent for many fields of human activity. As we know from numerous sources, the characteristic features of a weakly structured subject domain are as follows (see, for instance, [1]): it is problematic to provide a formal description and build analytical models; there are no benchmarks; all decisions made are unique ones; decision-making space dimensionality is very large; the domain is influenced by multiple significant criteria; information on the objects is incomplete, and human factor plays a considerable role.

At the same time, in order for decisions made in any subject domain (a weaklystructured one as well) to be efficient, they should be informed and wellsubstantiated. Thanks to consideration and systematization of all available information, the level of trustworthiness of the decision-maker (DM) increases, while the possibility of erroneous and incompetent decisions being made is reduced. So, in order to set priorities and plan respective activities, a DM needs to be able to analyze and formally describe weakly structured subject domains. Consequently, the problem of analysis and formal description of these domains retains its high relevance.

With the listed properties of weakly structured subject domains in mind, we should acknowledge that expert data-based methods and technologies are a powerful (and often, the only) mathematical tool for decision-making support in these domains. Experts (ideally – narrow-profile specialists) should be engaged, first, to outline a set of factors which are crucial for a given domain, and identify the nature of interrelations between these factors, and, second, to provide numeric (quantitative, cardinal), or at least, ordinal (rank) estimates of the relative weights of factors and alternative decision variants, from which the DM will have to select an optimal one.

In the most common case, decision-making means either choosing one of several alternative decision variants from a given set, or ranking/rating of these variants. Optimality of a decision variant (alternative) is defined based on some specific global (aggregate) efficiency criterion, which can reflect the degree of achievement of a certain main goal. Such general efficiency criterion is, usually, defined based on the realities of a specific situation. It provides the "starting point" in the process of formal analysis and decomposition (break-down) of the subject domain into particular aspects, as well as expert estimation of decision variants. In a way, the global efficiency criterion plays the role of a target function from mathematical optimization theory [2], or a utility function from utility theory [3]. However, we should stress that one of the peculiar features of weakly structured subject domains is the impossibility of analytic expression of this function. In fact, the experts are involved in order to define its specific (non-analytic!) look and an optimal decision variant (in accordance to a given efficiency criterion).

The result of expert decomposition of the main criterion (goal) into sub-criteria (sub-goals) is a hierarchy of criteria, which characterize the subject domain.

Expert data-based decision-support methods are listed and described in multiple publications. We can mention classical works by Kendall [4], Arrow [5], Kemeny [6], Fishburn [7], Saaty [8] and others. Soviet and Ukrainian authors (including Mirkin [9], Litvak [10], Totsenko [11], Gnatiienko and Snytiuk [12], and others) also largely

contributed to development of these methods. World-known multi-criteria decisionmaking methods include AHP/ANP [8], TOPSIS [13], ELECTRE [14], and others. In present-day Ukraine popular decision support methods include technological forecasting [15], complex target-oriented dynamic estimation of alternatives (CTDEA) [11, 16], and various interval estimation methods [12].

Acknowledged multi-criteria expert estimation methods include the aforementioned AHP, TOPSIS, ELECTRE, CTDEA methods; the most popular ranking aggregation methods include Borda rule, Condorced rule, Kemeny's median, and others; and when it comes to pair-wise comparisons, the common approaches include, again, AHP/ANP [8], "line", "triangle", "square" methods [11], and combinatorial approach [17, 18].

Specific applications of expert data-based methods, particularly those using the hierarchical approach to problem decomposition, are rather numerous. Dozens of specific applications are described in the proceedings of the International Symposiums for the Analytic Hierarchy Process (ISAHP) [19].

In modern-time Ukraine, there are several spheres, calling for expert data usage in decision-making process. In this context we can, again, mention the technological forecasting problems [15], socio-economic development planning [20], environmental protection [21], and other spheres. Warfare [22, 23] and information security and related decisions have gained relevance for Ukraine in recent years. Weakly-structured nature of these spheres is demonstrated in [24–26].

Another subject domain, which is relevant for Ukraine, is decision-making at the level of communities (village, raion, urban, territorial, etc). After launching of decentralization (particularly, budget decentralization), administrative-territorial organization reform, and formation of unified territorial communities (see [27, 28]) the role of communities in decision-making substantially increased. Consequently, there is a need for efficient yet easy-to-use analytic tools, which would provide an opportunity to consider the opinion of community representatives during decision-making. Only when public opinion is taken into account, community-level decisions will truly reflect the interests of community members. Specific decisions, immediately concerning community members, are related to such issues as planning and improvement of transport and road networks, domestic waste disposal, water supply and disposal, gentrification and improvement of territories, construction of recreation zones, reintegration of public usage locations (museums, libraries, parks, etc) into community life etc.

While the arsenal of available approaches and methods is seemingly wide, in this particular case we are talking about a specific type of problems and specific conditions of expert examination. So, the question is: which of the listed approaches (or their components) should be applied in community-level decision-making to ensure that community members' opinion is taken into account?

### 2 In Description of Problem Class and Solution Idea

The key feature of the aforementioned class of problems is their weakly structured nature. Formal problem statement is possible only when the goal, which the DM or other interested party is trying to achieve, is clearly defined. A community often finds it hard even to formulate a specific problem, not to mention identification of factors, which could influence its solution.

"What should be done with the waterfront area?", "how can we reorganize the park?", "what is the best way to arrange the system of water supply and water disposal in the settlement?", "what should we do with an old village cultural center (club), museum, library?" etc. Such typical community-level problem examples have several features in common. First, as it has been said, they immediately concern the representatives of a given community and reflect their interests. Second, they do not include any recommendations as to how the issue under consideration can be resolved. That is, the only input data is some problem to be solved, or some main goal to be achieved (let us denote it as G, and let us denote the main criterion of efficiency of its achievement as  $C_0$ ).

In view of weakly structured nature of the problems, it would be reasonable to hierarchically decompose the problem into specific components. Relevance and effectiveness of application of hierarchical approaches are shown, for example, in the works of Saaty ([8]), Totsenko ([11]), Gnatiienko and Snytiuk ([12]), Pankratova and Nedashkovskaya [29, 30], and others. The hierarchical approach proved to be an effective instrument in a multitude of applications (see [19]).

So, at the initial phase it is suggested to decompose (break-down) the main goal or problem into factors, which play decisive roles in its achievement (solution), as it is done in the listed methods, such as AHP [8], TOPSIS [13], or CTDEA [11, 16].

We should remember that formulations of criteria should be easy-to-understand, while criteria hierarchy graph should be balanced and not overloaded with excessive number of connections (edges) and nodes (more detailed requirements to the process of hierarchy building are described in [1, 31]).

Both in AHP and CTDEA, when a hierarchy is built, the weights of impact factors (criteria) are defined, that is every edge of the hierarchy graph is assigned a certain weight.

In [1, 31] it was stressed that the scale used for estimation of criteria had to be understandable for an unprepared expert or respondent. In order to achieve this, we should choose the scale with grades described by verbal rather than numeric values. Beside that, the scale should not make the respondent keep too many values and objects in mind simultaneously. For example, in a decision support technology, described in [32], the expert has to select the type of an ordinal pair-wise comparison ("more-less"), number of scale grades, and a particular grade from the chosen scale. This process calls for preliminary coaching sessions to be held with experts.

In order for the opinion of community members to be taken into account, they should be involved in the process of formal description of a given weakly structured problem. Moreover, the DM (or analytic research organizer) should keep in mind that, in

the general case, it is impossible to organize coaching sessions with all the respondents. So, the process of hierarchy building, particular look of the graph, specific criterion formulations, and the scale, in which the importance of criteria is estimated, should be as easy-to-understand as possible.

Based on these considerations, it is suggested to delegate the hierarchy building process to the experts in the given subject domain (as it is done in AHP or CTDEA), while introducing several additional requirements:

1) We should forbid input of cycles (loops, where criteria influence themselves) into the hierarchy graph. In the ideal case the hierarchy should represent a tree-type graph, that is, one node should have only one "ancestor" (hierarchy graphs of this type are addressed, for example, in [33, 34]).

2) Bottom-level criteria should be formulated not as concepts (for example, "quality of family leisure in the park, estimated in the scale from 1 to *n*"), but as positive statements, with which a respondent (not an expert, in the general case!) might agree or disagree. For example: "the park is a good place to spend quality time with a family"; response variants: "totally agree", "agree", "disagree", "totally disagree", "don't know". That is, we should provide respondents with an opportunity to estimate "atomic" bottom-level factors in Likert's scale [35]. Simplicity and vividness of this approach, as well as numerous sociological studies, in which the approach is successfully used, speak in its favor. Besides that, the choice of Likert's scale results from the need to consider opinions of a large quantity of respondents (and not just of a few experts, as in case of "classical" expert estimation methods).

3) Estimation of relative weights or impacts of factors (criteria) should be delegated to respondents from among target community members, so these estimates should be direct ones. In the process of weight estimation, in order to ensure vividness, the estimates are to be provided in graphic (and not verbal or numeric) format (this requirement is also based on the peculiarities of obtaining data from respondents, described in [1, 31]).

Based on the listed requirements, we can suggest the following step-by-step algorithm of formal description of a weakly structured problem.

#### 3 Step-by-step Algorithm of Problem Solution

1) The DM or expert examination organizer formulates the main problem or goal G and chooses the experts (at least one expert) in the respective subject domain.

2) Experts build a hierarchy of criteria (see Fig. 1 below), which are crucial for the given problem or goal:  $\{C_i : i = 0..n\}$ . The bottom-level criteria (which do not have ancestors in the hierarchy graph)  $\{C_{i_k} : k = 1..l\}$  are formulated as positive statements, which the respondents will estimate in Likert's agreement-disagreement scale.

3) A set of respondents  $\{r_j : j = 1..m\}$  is chosen from among the members of the given community.

4) Respondents estimate (directly, in clear, preferably, graphic format) the weights of impact factors at each hierarchy level. As a result, we get a set of impact coeffi-

cients (or relative weights)  $\{w_i^{(j)}: i = 1..n; j = 1..m\}$ , provided by every respondent.

Impact  $W_{i0}$  of criterion  $C_i$  upon the main criterion  $C_0$  is defined as shown in [11] (case of a hierarchy of "tree" or "network" type) and [34], according to formula (1).

$$w_{i0} = \sum_{p=1}^{n_i} \prod_{s=1}^{n_p} w_s \quad (1)$$

where  $n_i$  is the quantity of all possible paths from node  $C_i$  to node  $C_0$  in the criteria hierarchy graph; p is the number of a particular path;  $n_p$  is the length of the path number p, leading from  $C_i$  to  $C_0$ ; s is the number of the node within the path;  $w_s$  is the impact of criterion  $C_s$  upon its immediate ancestor in the path number p in the hierarchy graph.

We should note that if the hierarchy graph is a tree (every node (vertex) has no more than one ancestor, as on Fig. 1), the number of summands in formula (1) equals 1, as there is only one path, leading from any criterion  $C_i$  to the main criterion  $C_0$ .

5) Respondents select the estimates of bottom-level criteria in Likert's scale (as shown above). Scales grades are assigned the respective numeric equivalents for further aggregation, i.e., convolution (for instance, "6 - totally agree", "5 - agree", "4 rather agree than disagree", "3 - rather disagree than agree", "2 - disagree", "1 totally disagree", "0 - don't know or don't care"). As a result, we get a certain number of individual judgments of respondents for criteria from the bottom level of the hierarchy:  $\{q_{i_k}^{(j)}; k = 1..l; j = 1..m\}$ , where  $i_k$  are numbers of the bottom-level

criteria, l is their total number (quantity), and j is the respondent's number.

6) Estimates according to every criterion are aggregated through weighted summation (convolution) of estimates, provided by all respondents. As a result, we get the ratings of all bottom-level criteria  $Q_{i_{\mu}}$ ;

$$Q_{i_k} = \sum_{j=1}^m W_{i_k 0}^{(j)} q_{i_k}^{(j)}$$
 (2)

where  $w_{i_k0}^{(j)}$  is the relative impact of bottom-level criterion  $C_{i_k}$  upon the main criterion  $C_0$ , calculated according to formula (1) based on values of impacts of all intermediate-level criteria, provided by the respondent number j.

Based on these ratings, potential and priorities of the problem solution are identified, while community interests are taken into account. Highest-rated factors represent the top-priority aspects, which the community is satisfied with, while lowest-rated factors represent aspects, which do not satisfy the community, or are insignificant in the eyes of community members.

7) In order to check the consistency of respondents' judgments, we can ask them to write small verbal reviews, in which they should try to outline (once again, this time, verbally) positive and negative aspects, characterizing the subject domain.

We should stress that we are talking about inner consistency of judgments of each respondent: verbal review should be consistent with estimates, provided in Likert's scale at previous steps (see step 5). Mutual incompatibility of the estimates is not a problem, i.e. judgments of different respondents can differ, and it is quite natural, because in our case respondents only express their opinions, and do not try to estimate some objective values.

As judgments are provided in Likert scale, and it is only inner consistency of the estimates that is verified, traditional consistency measures (such as Kendall's rank correlation [4] for ordinal estimates, or consistency index (CI) and ration (CR) [8] for pair-wise comparisons, spectral consistency coefficient [11], double entropy index [36]) are not applicable. And that is why it makes sense for respondents to write verbal reviews.

8) In order to ensure transparency, tag (word) clouds can be generated (based on verbal reviews), which will also, in a way, represent the ratings of positive and negative aspects of the issue under consideration. In order to build tag clouds based on word frequency analysis of verbal review texts, publicly available online software tools can be used (such as WordItOut, Worlde, WordArt, WordCloud, TagUl, Many Eyes, Tagxedo, etc).

The final result of the algorithm is a formal analytic description of the subject domain. Such a description allows interested parties to clearly identify the key positive and negative aspects in the given subject domain, taking public opinion into account, and, thus, define its potential, prospects, and top-priority problems, at which resources should be targeted.

#### 4 Example

As an example of application of the suggested weakly structured subject domain description method, let us consider an actual research, which took place in summer of 2018, in one of the raion centers of Kyiv oblast (Ukraine). The main task was to study the quality of a public location (the territory of the state local history museum) in order to facilitate its further transformation and improvement. The study envisioned a set of tasks: 1) ensure communication (productive contact) between the community and the town management; 2) identify strong and weak points of the location; 3) identify priorities of the community (i.e. what was important for the residents); 4) evaluate the extent to which the location meets the needs and expectations of its users; 5) stimulate new ideas concerning location improvement; 6) define priorities of location development.

The focus-group from among the community members included 11 respondents, featuring local residents, museum employees, civil servants, journalists, artists.

The main goal was to improve the quality of the location; respectively, the generalized location quality was the main criterion.

Criteria hierarchy was built based on the SpaceShaper [37] methodology guidelines published by the British Commission for Architecture and Built Environment (CABE). SpaceShaper proved to be an effective, easy-to-use, and affordable instrument of public space improvement, particularly, in the British Commonwealth countries. Particular examples of successful application of the methodology for improvement of various public spaces can be found, for example, in [38–40]. In Ukraine different public organizations presently make the first attempts to use SpaceShaper methodology and its separate components for evaluation of quality and for transformation of public spaces.

The hierarchy of criteria, which influence the quality of the location, built in "So-lon" DSS [10, 39], is shown on Fig. 1.

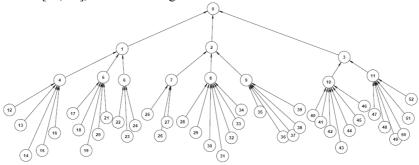


Fig. 1. The look of criteria hierarchy, built in "Solon" DSS

The list of criteria is presented in Table 1.

Table 1. The list of criteria from the hierarchy

#	Formulation
0.	Location quality
1.	Functionality
2.	Location characteristics
3.	Location value
4.	Accessibility
5.	Use
6.	Interests of residents (community members)
7.	Order
8.	Environment
9.	Design and look (appearance)
10.	Community (other people)
11.	You (individual respondent)
12.	It is easy to get here
13.	The place is easy-to-find
14.	Orientation is easy
15.	The place is open, whenever I come here
16.	I know what is happening here

18.   The place has everything I need     19.   I can enjoy the nature here     20.   Here I can learn a lot about local history, flora, fauna, art, etc     21.   The place helps me to keep healthy     22.   The place is popular among different people     23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is not noisy     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is inspiring     39.   The place is at home here     41. <t< th=""><th></th><th></th></t<>		
19.   I can enjoy the nature here     20.   Here I can learn a lot about local history, flora, fauna, art, etc     21.   The place is popular among different people     23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is in optrant component of the landscape     41.   The location is an important component of the landscape     42.   Everyone feels at home here     43.   It is a comfortable place for communication	17.	Here I can do what I want
20.   Here I can learn a lot about local history, flora, fauna, art, etc     21.   The place helps me to keep healthy     22.   The place is popular among different people     23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is inspiring     37.   You can witness the diversity of plants and animals here     38.   The place is nice     40.   The locatis are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is		4 , 0
21.   The place helps me to keep healthy     22.   The place is popular among different people     23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is worth visiting any time of the year     31.   The are to noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is inspiring     39.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place		
22.   The place is popular among different people     23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inportant component of the landscape     41.   The location is an important component of the landscape     41.   The locals are involved in location     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is sutractive for small business		
23.   A lot of different activities take place here     24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is worth visiting any time of the year     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small bus		
24.   There are no conflicts between different location users     25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is worth visiting any time of the year     30.   The place is not noisy     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is ninportant component of the landscape     41.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small b		
25.   It is clean here     26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here	23.	
26.   The place is cared for and looked after     27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is nell-lightord     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The location is an important component of the landscape     41.   The location is an important component of the landscape     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locatis are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can relax here     50.   The place is good for thinking     51.   I like being here	24.	There are no conflicts between different location users
27.   People, who take care about the location, are always available     28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is worth visiting any time of the year     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place is well-equipped     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The location is an important component of the landscape     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small business     47.   I feel well here     48.   I can relax here     50.   The place is good for thinking     <	25.	It is clean here
28.   Here you can hide from bad weather     29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is nice     40.   The location is an important component of the landscape     41.   The location is an important component of the landscape     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can reltax here     49.   I can reltax here     50.   The place is good for thinking     51.   I like being here	26.	The place is cared for and looked after
29.   The place is worth visiting any time of the year     30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The location is an important component of the landscape     41.   The location is an important component of the landscape     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locatis are proud of this place     45.   The place is well-located     46.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	27.	People, who take care about the location, are always available
30.   The place is well-lighted     31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The location is an important component of the landscape     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locats are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	28.	
31.   The air is clean     32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small business     47.   I feel well here     48.   I can relax here     50.   The place is good for thinking     51.   I like being here	29.	The place is worth visiting any time of the year
32.   The place is not noisy     33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	30.	The place is well-lighted
33.   I feel safe here     34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small business     47.   I feel well here     48.   I can relax here     50.   The place is good for thinking     51.   I like being here	31.	The air is clean
34.   I am totally satisfied with the location size     35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	32.	The place is not noisy
35.   The place adorns the neighborhood     36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	33.	I feel safe here
36.   The place is well-equipped     37.   You can witness the diversity of plants and animals here     38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	34.	I am totally satisfied with the location size
37.You can witness the diversity of plants and animals here38.The place is inspiring39.The place is nice40.The location is an important component of the landscape41.The locals are involved in location maintenance and organization of events on its territory42.Everyone feels at home here43.It is a comfortable place for communication44.The locals are proud of this place45.The place is well-located46.The place is attractive for small business47.I feel well here48.I can entertain myself here49.I can relax here50.The place is good for thinking51.I like being here	35.	
38.   The place is inspiring     39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	36.	The place is well-equipped
39.   The place is nice     40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	37.	You can witness the diversity of plants and animals here
40.   The location is an important component of the landscape     41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	38.	The place is inspiring
41.   The locals are involved in location maintenance and organization of events on its territory     42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	39.	The place is nice
42.   Everyone feels at home here     43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	40.	The location is an important component of the landscape
43.   It is a comfortable place for communication     44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	41.	The locals are involved in location maintenance and organization of events on its territory
44.   The locals are proud of this place     45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	42.	Everyone feels at home here
45.   The place is well-located     46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	43.	It is a comfortable place for communication
46.   The place is attractive for small business     47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	44.	The locals are proud of this place
47.   I feel well here     48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	45.	The place is well-located
48.   I can entertain myself here     49.   I can relax here     50.   The place is good for thinking     51.   I like being here	46.	The place is attractive for small business
49. I can relax here   50. The place is good for thinking   51. I like being here	47.	I feel well here
50. The place is good for thinking   51. I like being here	48.	I can entertain myself here
51. I like being here	49.	I can relax here
51. I like being here	50.	The place is good for thinking
52. I come here to hide (escape) from routine	51.	
· · · · · · · · · · · · · · · · · · ·	52.	I come here to hide (escape) from routine

As we can see, the topmost (first) level of the hierarchy consists only of the main criterion "the overall quality (efficiency) of the location". Its immediate sub-criteria (descendants) are functionality (which, in turn, includes accessibility, ease of use, and interests of residents), characteristics (including order, environment, and look/appearance/design), and value of the location (for the community and an individual respondent respectively). The bottom (fourth) level features 41 criterion, formulated as positive statements, with which respondents can agree or disagree (for instance, sub-criteria of accessibility are: "it is easy to get here", "the place is open whenever I come here" etc).

Every respondent received a questionnaire form, in which (s)he had to specify his(her) occupation and location usage mode (frequency and purpose of visits), provide weights of criteria of the second and third levels of the hierarchy, and estimate the bottom-level criteria in Likert's agreement-disagreement scale.

Estimation of weights of intermediate-level criteria was performed using sector diagrams (pie charts) (see Fig. 2). The choice of this particular method for weight estimation results, primarily, from simplicity and transparency considerations. As a result of estimation, every second-level criterion was assigned an integer-value weight from 0 to 12 (sum of all second-level criterion weights equals 12), while every third-level criterion was assigned a weight from 0 to 144 (sum of all third-level criterion weights equals 144). Weights of these criteria were estimated by each respondent. It should be stressed, that this particular method of criterion weight estimation was chosen for the specific study. In the general case, depending on specific hierarchy structure, and the degree of process automation, other weight input methods can be used, providing they are clear and understandable.

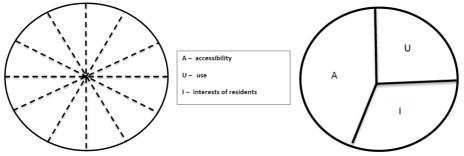


Fig. 2. An example of criterion weight input using pie chart

Bottom-level criteria were presented to respondents in the form of tables (in accordance to SpaceShaper methodology, their weights are considered equal). Respondents had to express their judgment on each of the 41 bottom-level criterion in Likert's scale. An example of the table from the questionnaire, filled out by every respondent, is shown in Table 2.

Once the surveys were completed, the respondents were offered to describe in their own words the strong and weak points of the location, as well as their vision of the ideal condition of the location (so-called "letter from the future"). Aggregation of survey data was performed as follows.

Verbal values were replaced by numeric equivalents (as shown in the previous section): 6 - totally agree", "5 - agree", "4 - rather agree than disagree", "3 - rather disagree than agree", "2 - disagree", "1 - totally disagree", "0 - don't know or don't care".

After that rating of every bottom-level criterion was calculated through weighted summation (convolution) of estimates provided by all respondents (according to formula (2)).

In general case bottom-level ratings lie within the range between 0 and  $R_{\text{max}}$ :

$$R_{\max k} = mq_{\max} w_{\max k}, (3)$$

where k is the number of bottom-level criterion; m is the quantity of respondents;  $q_{\text{max}}$  is the maximum value of numeric equivalent of a scale grade, which can be chosen by a respondent, while  $w_{\text{max}\,k}$  is a maximum possible criterion weight value.

	Totally agree	Agree	Rather agree	Rather disagree	Disagree	Totally disagree	Don't know	Don't care
Accessibility								
It is easy to get here								
The place is easy-to-find								
Orientation is easy								
The place is open, whenever I come here							-	
I know what is happening here							-	
Use							-	
Here I can do what I want							-	
The place has everything I need								
I can enjoy the nature here							-	
Here I can learn a lot about local history, flora, fauna,								
art etc								
The place helps me to keep healthy							-	
Interests of residents (community)							-	
The place is popular among different people								
A lot of different activities take place here								
There are no conflicts between different location users								

In the case of our particular problem the number of respondents is m = 11; the range of bottom-level criterion weights is

$$\{w_{i_k} \in Z \cap [0;144]; \sum_{k=1}^{i} w_{i_k} = w_{\max} = 144; l = 41; i_k = \{12..52\}\}, \text{ i.e. bottom-}$$

level criteria from Table 1 with numbers 12 to 52 can be re-numbered from 1 to 41; their weights are expressed by integer values from 0 to 144, and their sum equals 144. The range of numeric equivalents of Likert scale grades lies between "0" ("don't know or don't care") and "6" ("totally agree"), i.e in formula (3)  $q_{\rm max} = 6$ . Respectively, bottom-level criterion ratings will belong to the range from 0 to 9504 (according to (3)  $R_{\rm max} = 11 \times 6 \times 144 = 9504$ ). If all ratings need to fall within the range between 0 and 1, they can be normalized.

Bottom-level criterion ratings, obtained through aggregation of respondents' estimates, are shown on Fig. 3. For the sake of convenience these criteria are numbered from 1 to 41 (as described above).

We should note that absolute rating value does not play any significant role. It is the ratios (or differences) between ratings of different criteria that matter. Besides that, important information can be obtained from the ratios of ratings within each subgroup (functionality, characteristics, value of location). Fig.4 displays the relative ratings of criteria, which belong to "functionality" subgroup.

Similarly, the respective ratings for each intermediate-level criterion were calculated. Rating of a criterion which has descendants in the hierarchy graph is calculated as the weighted sum of ratings of its immediate sub-criteria:

$$Q_{i} = \sum_{j=1}^{m} Q_{i}^{(j)} = \sum_{j=1}^{m} \sum_{k=1}^{\nu} w_{i_{k},i}^{(j)} Q_{i_{k}}^{(j)} , \qquad (4)$$

where  $Q_i$  is the rating of criterion  $C_i$ ;  $Q_i^{(j)}$  is the rating of this criterion calculated based on estimates provided by respondent number j; m is the total number of respondents; v is the number of immediate sub-criteria of  $C_i$  in the hierarchy graph;  $w_{i_k,i}^{(j)}$  is the weight of impact of sub-criterion number  $i_k$  upon criterion  $C_i$ , estimated by respondent number j;  $Q_{i_k}^{(j)}$  is the rating of the sub-criterion number  $i_k$ , calculated based on estimates provided by respondent number j. For instance, in the hierarchy on Fig. 1 the sub-criteria of "Functionality" ( $C_1$ ) are "Accessibility" ( $C_4$ ), "Use ( $C_5$ ), and "Interests of community" ( $C_6$ ). So, the rating of "Functionality" is calculated as the sum of ratings of these sub-criteria.

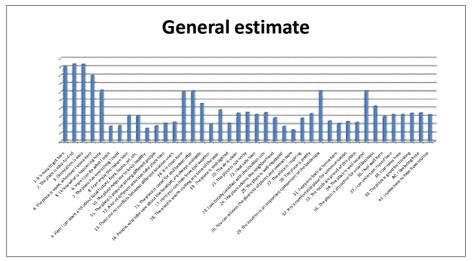
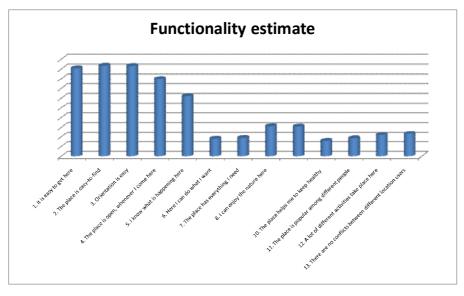


Fig. 3. Relative ratings of 41 bottom-level criteria

Aggregate relative ratings of third-level criteria are shown on Fig. 5, illustrating respondents' opinion about location's compliance with the parameters listed in the survey. As we can see from the diagram, the weakest points of the location are that (according to the respondents) it does not meet the needs of the community and is rarely used.

Based on textual analysis of verbal reviews and "letters from the future", tag clouds were built. It is interesting to note that the drawbacks, mentioned by respondents in verbal reviews, confirm the ratings, shown on Fig. 5 (i.e., respondents' judg-



ments are rather consistent): according to the respondents, low level of location usage and its inability to serve community interests, are the main flaws of the location.

Fig. 4. Functionality of location: relative ratings of criteria

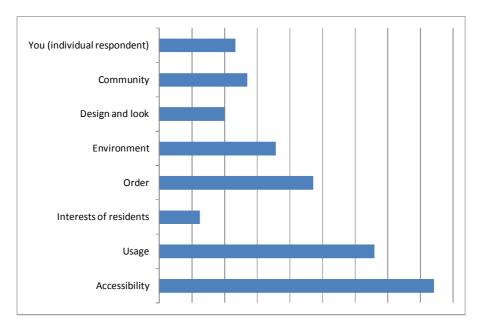


Fig. 5. Generalized ratings of third-level criteria

Aggregate survey results allow us to make several important conclusions.

1. Location has a great potential for further improvement and development. Community representatives consider themselves capable of active participation in transformation of the public space.

2. Museum space and adjacent territory are not the focal point of active community life. With the exception of museum employees, community residents rarely visit the location.

3. The main advantages of the public space are convenient downtown location, coziness, presence of greenery, open territory, and esthetic attractiveness of the historical museum building. The main drawbacks (and, consequently the main points for location development) include poor understanding of its designation by the community, lack of cultural events, activities, entertainment, management initiatives, creativity; alerting condition of trees on the territory of the museum.

4. While accessibility (convenient location), attractiveness for the community, and environmental potential are the strong points of the space, inclusiveness (consideration of interests of all potential user categories), full-fledged utilization of location's capacity, design/look, and infrastructure are the top-priority development aspects.

5. Transformation and sustainable development of the location should be based on the results of the conducted study, particularly, on aggregate judgments of the respondents from among community members. Location development activities and projects, implemented by local authorities, NGOs, activists, volunteers, based on public opinion, will be successful and get support from the community.

As of now, public organizations in cooperation with local activists and authorities have already accomplished several projects along the lines of the study results.

# 5 Peculiar Features of the Approach: Place in Decision Science, Advantages and Disadvantages

As we can see, the described approach is a "hybrid" one in a way that it combines the elements of both decision theory and sociology (surveying, agreement scale usage).

The following features of the approach are common with the available decision support methods:

— usage of hierarchic problem decomposition (as in AHP [8] and CTDEA [11, 16]);

— heuristic transition from verbal judgments (like "agree/disagree") to numeric values (in the example – from "0" to "6"). Such a transition, in one form or the other, happens, virtually, in all multi-criteria alternative estimation methods that feature linear convolution (weighted summation) of ordinal or cardinal values (including Borda, Condorcet, AHP, TOPSIS, CTDEA, etc), because, as Litvak showed in [10], the necessary and sufficient condition of existence of an aggregate criterion (convolution across its sub-criteria) is expression of alternative estimates according to these sub-criteria in the ratio scale;

 aggregation (generalization, in our case through linear convolution) of data across multiple criteria, obtained from multiple respondents;  verification of consistency of judgments (in our case – through informal analysis of verbal reviews).

Now let us list the main differences of the approach from the existing methods.

— the key task is only to describe the subject domain, i.e. to form a system of linked criteria (not to compare alternatives or projects according to these criteria, as it is done in AHP or CTDEA);

— the way of criterion formulation. "Atomic" bottom-level criteria, which do not have descendants in the hierarchy graph, are formulated as positive statements (and not definitions, as in traditional methods), with which a respondents can agree or disagree;

 as a result, instead of direct estimates or pair-wise comparisons, Likert's agreement scale is used;

— ease of problem decomposition: hierarchy graph is a "tree" [33, 34]; a networktype structure, i.e. a graph, in which any node can have more than one ancestor, can be too complex to be perceived by respondents;

— no need for coaching sessions with respondents (thanks to simplicity and transparency of the method).

So, we should stress once more that the key feature of the method is the combination of expert and sociological mindsets, which ensures, on the one hand, ease of use, and on the other – high efficiency of the method.

The results of the method's work are the ratings of activity scopes, providing the basis for further prioritization and, potentially, for allocation of limited resources [21].

The method's advantages are ease-of-use and understandability for a community member, efficiency and transparency, universality and flexibility (for each new subject domain a new unique hierarchy can be built), vividness of subject domain description process and representation of results.

The method's key disadvantages are the possibility of manipulations (experts can formulate criteria in some biased way, however, this is the issue of ethical principles of these experts and the DM), and of emergence of "lobbies" among community members (according to profession, age, mindset, gender, wealth, social status, etc).

A separate problem concerns manual input and processing of data (when MS Excel is the only software tool used for data aggregation). Ideally, the process of formal description of subject domain should be almost fully automated. Certain steps of the above-listed algorithm are already automated within the existing DSS. Particularly, "Consensus-2" DSS [42] includes means for registration of experts who are inputting the hierarchy, and for input of the hierarchy itself. "Solon" DSS [11, 41] includes tools for hierarchy input, as well as for calculation of relative impacts of criteria. Thus, the functions, delegated to experts, are already automated, while functions, delegated to respondents and to the research organizer (knowledge engineer, who has to aggregate the data and obtain recommendations for the DM using the DSS tools) still require automation. In order to simplify the process of surveying and aggregation of survey data is would be reasonable to automate:

- completion of the surveys (for example, using tablets or similar gadgets);

- submission of survey data to DSS knowledge base in remote mode;

— calculation of criterion ratings using the mathematical tools of a DSS.

Recognition and frequency analysis of verbal review texts, as well as tag cloud building are a bit more difficult to automate, however improvement of this algorithm step is no less relevant than automation of other steps.

# 6 Conclusions

It has been shown that community-level problems represent an example of weakly structured subject domains. During their formal description we should consider both expert data and community members' opinion. In view of the need to consider public opinion during community-level decision-making, it is unreasonable to apply existing decision support methods and technologies in their classical form.

An efficient, yet simple, method has been suggested for formal description and analysis of community-level problems, taking public opinion into consideration. The method allows a DM, a local authority, an NGO, community representatives, volunteers, activists, media, or any other interested parties to get a clear understanding of a specific subject domain, which will provide the basis for prioritizing of future steps.

Experimental results have been obtained, based on conducted research of quality of a specific public space. The research confirms both efficiency and ease-of-use of the suggested approach. Based on the research results, specific recommendations concerning improvement of the target public space (location) have been worked out.

The described method should be used for community-level decision-making – in villages, raions, towns, neighborhoods — in spheres, immediately concerning the respective community members. Particular decisions might concern such aspects as planning and improvement of road and transport networks, domestic waste disposal, water supply and disposal, planning and improvement of territories, reintegration of public spaces into active community life, neutralization of negative information impacts, etc.

The method is an efficient decision support tool, which should be used by local self-government bodies, civil organizations, volunteers, activists, and any other interested parties.

Further studies will be dedicated to search for new applications of the method, and to automation of particular steps of the described procedure of analysis of weakly structured subject domains.

#### References

- Kadenko S.V. Prospects and Potential of Expert Decision-making Support Techniques Implementation in Information Security Area; in Selected Papers of the XVIIIII International Scientific and Practical Conference on Information Technologies and Security (ITS 2016) Kyiv 2016/ CEUR Workshop Proceedings, pp. 8-14 (2016).
- 2. Boyd S., Vandenberghe L. Convex Optimization. Cambridge University Press (2004).
- Keeney R.L., Raiffa H. Decisions with Multiple Objectives: Preferences and Value Tradeoffs Cambridge University Press. (1993).
- 4. Kendall, M. A New Measure of Rank Correlation. Biometrika. 30 (1-2), pp. 81-89 (1938).

- 5. Arrow K. J. Social Choice and Individual Values, 2nd ed. New York: Wiley (1963).
- John G. Kemeny. Mathematics without Numbers. *Daedalus*. Vol. 88, No. 4, pp. 577-591 (1959).
- 7. Fishburn P.C. Utility Theory for Decision Making. Wiley (1970).
- 8. Saaty, T.L. Fundamentals of Decision Making and Priority Theory with The Analytic Hierarchy Process. RWS Publications, Pittsburgh PA (1994).
- 9. Миркин Б.Г. Проблема группового выбора. М. Наука (1974).
- Литвак Б. Г. Экспертная информация. Методы получения и анализа. М.: Радио и свіязь (1982).
- Тоценко В.Г. Методы и системы поддержки принятия решений. Алгоритмический аспект. ИПРИ НАНУ. К.: Наукова думка (2002).
- Гнатієнко Г. М., Снитюк В.Є. Експертні технології прийняття рішень. К.: ТОВ "Маклаут" (2008).
- 13. Hwang, C. L., Yoon K. Multiple attribute decision making: methods and applications : a state-of-the-art survey. Berlin; New York : Springer-Verlag (1981).
- Roy, Bernard. Classement et choix en présence de points de vue multiples (la méthode ELECTRE). La Revue d'Informatique et de Recherche Opérationelle (RIRO). (8): pp. 57– 75 (1968).
- 15. M.Z.Zgurovsky, Yu.P.Zaychenko. The Fundamentals of Computational Intelligence: System Approach. Studies in Computational Intelligence, 652. Springer. (2005).
- Циганок В. В. Удосконалення методу цільового динамічного оцінювання альтернатив та особливості його застосування. Реєстрація, зберігання і оброб. даних. Т. 15, № 1. С. 90-99 (2013).
- Tsyganok V., Kadenko S., Andriichuk O., Roik P. Combinatorial Method for Aggregation of Incomplete Group Judgments. IEEE First International Conference on System Analysis & Intelligent Computing (SAIC), DOI: 10.1109/SAIC.2018.8516768, pp. 25-30 (2018).
- Tsyganok V. Investigation of the aggregation effectiveness of expert estimates obtained by the pairwise comparison method. Mathematical and Computer Modeling. 52(3-4). pp. 538–544 (2010).
- 19. Proceedings of the International symposium for the analytic hierarchy process (archive). http://www.isahp.org/proceedings/, last accessed 2018/11/15.
- Терентьєв О. М., Просянкіна-Жарова Т.І., Савастьянов В.В. Використання засобів текстової аналітики як інструменту оптимізації підтримки прийняття рішень у задачах розробки планів соціально-економічного розвитку України. Реєстрація, зберігання і оброб. даних..Т. 18, № 3. сс. 75-86 (2016).
- Tsyganok. V., Kadenko S., Andriichuk O., Roik P. Usage of multicriteria decision-making support arsenal for strategic planning in environmental protection sphere. Journal of Multicriteria Decision Analysis. Vol. 24, Issue 5-6, pp. 227-238 (2017).
- Чепков І.Б., Ланецкий Б.М., Леонтьєв О.Б., Лук'янчук В.В. Методичний підхід до обгрунтування раціонального співвідношення обсягів розробки, закупівлі та ремонту озброєння й військової техніки. Озброєння та військова техніка. No 3. C. 9–14 (2014).
- Циганок В.В., Каденко С.В., Андрійчук О.В., Качанов П.Т., Роїк П.Д. Інструментарій підтримки прийняття рішень як засіб стратегічного планування. Озброєння та військова техніка. № 3(7). С. 59-66 (2015).
- Горбулін В.П., Додонов О.Г., Ланде Д.В. Інформаційні операції та безпека суспільства: загрози, протидія, моделювання: монографія. К., Інтертехнологія (2009).
- Додонов А.Г., Ландэ Д.В., Цыганок В.В., Андрейчук О.В., Каденко С.В., Грайворонская А.Н. Распознавание информационных операций. Киев. (2017).

- Kadenko S.V. Defining Relative Weights of Data Sources during Aggregation of Pair-wise Comparisons. Selected Papers of the XVII International Scientific and Practical Conference on Information Technologies and Security (ITS 2017) Kyiv 2017. pp. 47-55 (2017).
- 27. Закон України Про добровільне об'єднання територіальних громад (Відомості Верховної Ради (ВВР), 2015, № 13, ст.91). http://zakon5.rada.gov.ua/laws/show/157-19, last accessed 2018/11/15.
- Розпорядження Кабінету Міністрів України від 1 квітня 2014 р. № 333-р «Про схвалення Концепції реформування місцевого самоврядування та територіальної організації влади в Україні». http://zakon0.rada.gov.ua/laws/show/333-2014-%D1%80, last accessed 2018/11/15.
- Pankratova, N.D. & Nedashkovskaya, N.I. Hybrid Method of Multicriteria Evaluation of Decision Alternatives. Cybern Syst Anal 50: 701. https://doi.org/10.1007/s10559-014-9660-2 (2014).
- N.D.Pankratova & N.I.Nedashkovskaya. A decision support system for evaluation of decision alternatives on basis of a network criteria model. 2017 IEEE First Ukraine Conference on Electrical and Computer Engineering (UKRCON). DOI: 10.1109/UKRCON.2017.8100363 (2017).
- 31. Каденко С.В. Проблеми представлення експертних даних у системах підтримки прийняття рішень. Реєстрація, зберігання і обробка даних. Т. 18 № 3, С. 67-74 (2016).
- Tsyganok, V.V., Kadenko, S.V., & Andriichuk, O.V. Using Different Pair-wise Comparison Scales for Developing Industrial Strategies. Int. J. Management and Decision Making. 14(3), pp 224-250 (2015).
- 33. Saaty, T.L. The Analytic Hierarchy Process. McGraw-Hill, New York. (1980).
- Kadenko S.V. Determination of Parameters of Criteria of «Tree» Type Hierarchy on the Basis of Ordinal Estimates. Journal of Information and Automation Sciences. Vol. 40. i.8. P. 7–15 (2008).
- Likert R. A Technique for the Measurement of Attitudes. Archives of Psychology. # 140. P. 1–55 (1932).
- Olenko A., Tsyganok V. Double Entropy Inter-Rater Agreement Indices. Applied Psychological Measurement 40(1). pp. 37–55 (2016).
- SpaceShaper User's Guide. https://www.designcouncil.org.uk/resources/guide/ spaceshaper-users-guide, last accessed 2018/11/15.
- St. James Park, Southampton. CABE Spaceshaper Workshop Facilitators Report. http://www.westleydesign.co.uk/what-we-do/Downloads/WestleyDesign-StJamesSpaceshaper.pdf, last accessed 2018/11/15.
- 39. Camberwell Town Centre Spaceshaper Consultation Report. https://www.southwark.gov.uk/assets/attach/4070/Camberwell\_Town\_Centre\_Spaceshap er\_Consultation\_Report\_December\_2011.pdf, last accessed 2018/11/15.
- 40. Carawatha Park Spaceshaper Workshops. http://www.melvillecity.com.au/static/ attachments/2013/April/3383\_SpaceShaper\_Report.pdf, last accessed 2018/11/15.
- 41. Тоценко В.Г., Качанов П.Т., Циганок В.В. Комп'ютерна програма «Система підтримки прийняття рішень «Солон-3» (СППР «Солон-3»). Свідоцтво про реєстрацію авторського права на твір № 8669 від 31.10.2003 (2003).
- 42. Циганок В.В., Роїк П.Д., Андрійчук О.В., Каденко С.В. Комп'ютерна програма «Система розподіленого збору та обробки інформації для систем підтримки прийняття рішень «Консенсус-2» (СРЗОІ «Консенсус-3»). Свідоцтво про реєстрацію авторського права на твір № 75023 від 27.11.2017 (2017).