WebIsAGraph: A Very Large Hypernymy Graph from a Web Corpus

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Abstract

In this paper, we present WebIsAGraph, a very large hypernymy graph compiled from a dataset of *is-a* relationships extracted from the CommonCrawl. We provide the resource together with a Neo4j plugin to enable efficient searching and querying over such large graph. We use WebIsAGraph to study the problem of detecting polysemous terms in a noisy terminological knowledge graph, thus quantifying the degree of polysemy of terms found in *is-a* extractions from Web text.

1 Introduction

Acquiring concept hierarchies, i.e., taxonomies from text, is a long-standing problem in Natural Language Processing (NLP). Much previous work leveraged lexico-syntactic patterns, which can be either manually defined (Hearst, 1992) or automatically learned (Shwartz et al., 2016). Pattern-based methods were shown by (Roller et al., 2018) to outperform distributional methods, and can be complemented with state-of-the-art meaning representations such as hyperbolic embeddings (Nickel and Kiela, 2017) to infer missing *is-a* relations and filter wrong extractions (Le et al., 2019). Complementary to these efforts, researchers looked at ways to scale hypernymy detection to very large, i.e., Web-scale corpora (Wu et al., 2012). Recently, (Seitner et al., 2016) applied Hearst patterns to the CommonCrawl¹ to produce the WebIsaDb. Using Web corpora makes it possible to produce hundreds of millions of isa triples: the extractions, however, include many false positives and cycles (Ristoski et al., 2017).

Methods for hypernym detection like, e.g., pattern-based approaches, have a limitation in that they do not necessarily produce proper taxonomies (Camacho-Collados, 2017): automatically detected is-a relationships, on the other hand, can be used as input to taxonomy induction algorithms (Velardi et al., 2013; Faralli et al., 2017; Faralli et al., 2018, inter alia). These algorithms rely on the topology of the input graph, and, therefore, cannot be applied 'as-is' to Webscale resources like WebIsaDb, since this resource merely consists of a set of triples. Moreover, WebIsADb does not contain fully semantified triples, i.e., subjects and objects of the is-a relationships consist of potentially ambiguous terminological nodes. This is because, due to their large size, source input corpora like the CommonCrawl cannot be semantified upfront. Linking to the semantic vocabulary of a reference resource like DBpedia (Hertling and Paulheim, 2017) also barely mitigate this problem, since Wikipedia-centric knowledge bases have not, and cannot be expected to have, complete coverage over Web data (Lin et al., 2012).

In this paper, we present an initial solution to these problems by building the first very large hypernymy graph, dubbed WebIsAGraph, built from is-a relationships extracted from a Web-scale cor-This is a relevant task: although Wordpus. Net (and other thesauri) already provides a catalog of ambiguous terms, many nodes of WebIsA-Graph are not covered in available lexicographic resources, because they are proper names, technical terms, or polysemantic words. Our graph which we make freely available to the research community to foster further work on Web-scale knowledge acquisition - is built from the WebIsADb on top of state-of-the-art graph mining tools²: thanks to an accompanying plugin, it can be easily searched, queried, and explored. We-

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¹http://commoncrawl.org

²Neo4j: https://neo4j.com/

bIsAGraph may represent an opportunity to researchers for investigating approaches to a variety of tasks on large automatically acquired term tuples. As an example, we use our resource to investigate the problem of identifying ambiguous terminological nodes. To automatically detect whether a lexicographic node is ambiguous or not, we use information from both the graph (topological features) and textual labels (word embeddings) as features to train a model using supervised learning. Our results provide a first estimate of the degree of polysemy that can be found among *is-a* relationships from the Web.

2 Creating WebIsAGraph

We created a directed hypernymy graph from the WebIsADb (Seitner et al., 2016). WebIsADb is a Web-scale collection of noisy hypernymy relations harvested with 58 extraction patterns and consisting of 607,621,170 tuples. Since the aim of WebIsADb was to study the behaviour (on a large scale) of Hearst-like extraction patterns, rather than collecting relations with high precision, in order to reduce noise (false positives) we preselected the top-20 more precise extraction patterns in (2016) from the original 58 and identified 385,459,302 tuples.

After removing matches with a frequency lower than 3 and isolated nodes, i.e., nodes with degree equal to 0, we obtained a directed graph consisting of 33,030,457 nodes and 65,681,899 directed edges (see Table 1). The generation of such a large graph required several weeks of computation on a quad-core machine with 32 GB of RAM, using a state-of-the art graph-db system, like Neo4j. Note that the inherent sequential nature of the task of indexing tuples, nodes and edges does not benefit from the use of parallel computation. Next, we developed efficient tools for graph querying, which are released to the community, and described in https://sites.google.com/ unitelmasapienza.it/webisagraph/, where we also include examples of queries.

3 Measuring the polysemy of WebIsAGraph

Let $p_{SI}(n)$ be the function that predicts if a terminological node *n* corresponds to a *monosemous* or a *polysemous* concept. We leverage a companion sense inventory as a ground truth, and we train different classifiers with a combination of topological

WebIsAGraph							
nodes	33,030,457						
edges	65,681,899						
weakly connected components	3,099,898						
nodes of largest component	26,099,001						
Avg. node Degree	3.97						

Table 1: Structural statistics of WebIsAGraph

and textual features, described hereafter.

Topological features. Our conjecture is that in a taxonomy-like terminological graph (even a noisy one) there is a correlation between the mutual connectivity of a node neighborhoods and its polysemy. For example, consider the polysemous word machine - which, according to WordNet, has at least six heterogeneous meanings, ranging from the 'any mechanical or electrical device' to 'a group that controls the activities of a political party' - and the monosemous word *floppy disk*. We expect to observe a different degree of mutual connectivity across the corresponding incoming and outgoing nodes. In particular, for monosemous words, we expect a higher mutual connectivity. With reference to Figure 1, left side, the two hypernyms of "floppy disk": "memory" and "data storage", have also "RAM" as a common hyponym. In contrast, nodes in the direct neighborhood of "machine" (leftmost graph in Figure 1) do not have mutual connections.

Our aim is thus to identify topological features that may help quantifying the previously described connectivity properties. To cope with scalability, we consider topological features built on top of 1-hop/2-hop sub-graphs of a node n. Hence, we identify two induced sub-graphs $G^{-+}(n)$ and $G^{+-}(n)$, induced on $V^{-+}(n) = In(n) \cup_{v \in In(n)} Out(v)$ and $V^{+-}(n) = Out(n) \cup_{v \in Out(n)} In(v)$ respectively, where In(x) and Out(x) are the sets of incoming and outgoing nodes of x (including x). Next, we remove from these sub-graphs the node n, and compute the following features:

- $cc_{G^{-+}}(n)$ and $cc_{G^{+-}}(n)$: the resulting number of weakly connected components;
- $v_{G^{-+}}(n)$ and $v_{G^{+-}}(n)$: the resulting number of nodes;
- $e_{G^{-+}}(n)$ and $e_{G^{+-}}(n)$: the resulting number of edges.

With reference to the example of Figure 1, the light gray sub-graph (a) is $G^{-+}(n)$, the dark sub-



Figure 1: An example excerpt of the neighborhood induced sub-graphs for "machine" and "floppy disk", (a) $G^{-+}(n)$ in gray and (b) $G^{+-}(n)$ in dark gray. Dashed edges connect each n with its hypernyms and hyponyms.

graph (b) is $G^{+-}(n)$, and furthermore for n ="machine": $cc_{G^{-+}}(n) = 2$, $cc_{G^{+-}}(n) = 2$, $v_{G^{-+}}(n) = 5$, $v_{G^{+-}}(n) = 5$, $e_{G^{-+}}(n) = 3$, and $e_{G^{+-}}(n) = 3$, while for the n ="floppy disk": $cc_{G^{-+}}(n) = 1$, $cc_{G^{+-}}(n) = 1$, $v_{G^{-+}}(n) = 4$, $v_{G^{+-}}(n) = 2$, $e_{G^{-+}}(n) = 3$, and $e_{G^{+-}}(n) = 1$.

Textual features. Similarly to topological features, our hypothesis is that textual features of the neighborhood nodes should exhibit a lower average similarity when n is polysemous. We extract textual features on top of pre-trained word embeddings, widely adopted in many NLP-related tasks (Camacho-Collados and Pilehvar, 2018). Formally, given a node n:

• $\overline{W}(n)$ is the word embedding vector of n computed as follows:

$$\vec{W}(n) = \frac{\sum_{t \in tokens(n)} \vec{we}(t)}{|tokens(n)|} \tag{1}$$

where tokens(n) is the function that retrieves the set of tokens composing the word n (e.g., if $n = hot \ dog, \ tokens(n) = \{hot, \ dog\}$), and $\overrightarrow{we}(t)$ is a pre-trained word embedding vector;

 Δ_{in}(n) and Δ_{out}(n): the cosine similarity between W(n) and the average word embeddings vector of incoming and outgoing nodes of n respectively;

$$\Delta_{in}(n) = CosSim(\vec{W}(n), \frac{\sum_{m \in In(n)} \vec{W}(m)}{|In(n)|}) \quad (2)$$

$$\Delta_{out}(n) = CosSim(\vec{W}(n), \frac{\sum_{m \in Out(n)} \vec{W}(m)}{|Out(n)|})$$
(3)

		Features								
		t	opologica		textual		all			
	Algo.	P	R	F_1	P	R	F_1	P	R	F_1
	Rnd	0.47	0.47	0.47	0.47	0.47	0.47	0.47	0.47	0.47
		$\pm .05$	$\pm .05$	$\pm .05$	±.05	$\pm .05$				
WordNet	NN	0.61	0.61	0.60	0.72	0.72	0.72	0.73	0.73	0.73
		$\pm .02$	$\pm.02$	$\pm .02$	±.03	$\pm.03$	$\pm.02$	$\pm.04$	$\pm.04$	$\pm.04$
	ABC	0.62	0.62	0.62	0.67	0.67	0.67	0.70	0.70	0.70
		$\pm .03$	$\pm.03$	$\pm.03$	±.02	$\pm.02$	$\pm.01$	$\pm.03$	$\pm.03$	$\pm.03$
	GBC	0.62	0.62	0.62	0.69	0.68	0.68	0.72	0.71	0.71
		$\pm .02$	$\pm.02$	$\pm.02$	±.01	$\pm.01$	$\pm.01$	$\pm .03$	$\pm.03$	$\pm.03$
DBpedia	Rnd	0.51	0.51	0.51	0.51	0.51	0.51	0.51	0.51	0.51
		$\pm .03$	$\pm.03$	$\pm.03$	±.03	$\pm.03$	$\pm.03$	$\pm .03$	$\pm.03$	$\pm.03$
	NN	0.60	0.60	0.59	0.73	0.73	0.73	0.74	0.74	0.74
		$\pm.01$.01	$\pm.01$	±.03	$\pm.03$	$\pm.03$	$\pm .03$	$\pm.03$	$\pm.03$
	ABC	0.60	0.60	0.60	0.69	0.69	0.69	0.71	0.71	0.71
		$\pm .02$	$\pm.02$	$\pm .02$	±.02	$\pm.02$	$\pm.02$	$\pm.04$	$\pm.04$	$\pm.04$
	GBC	0.61	0.61	0.61	0.70	0.70	0.70	0.73	0.73	0.73
		$\pm .02$	$\pm .02$	$\pm .02$	±.03	$\pm.03$	$\pm.03$	$\pm .02$	$\pm.02$	$\pm.02$
-	Rnd	0.50	0.50	0.50	0.50	0.50	0.50	0.50	0.50	0.50
edi		$\pm .01$	$\pm.01$	$\pm.01$	±.01	$\pm.01$	$\pm.01$	$\pm .01$	$\pm.01$	$\pm.01$
VordNet∪DBpc	NN	0.54	0.53	0.50	0.70	0.70	0.70	0.71	0.70	0.70
		$\pm .03$	$\pm .05$	$\pm.12$	±.02	$\pm.02$	$\pm.02$	$\pm .02$	$\pm.01$	$\pm.01$
	ABC	0.55	0.55	0.55	0.64	0.64	0.64	0.65	0.65	0.65
		± 0.02	± 0.02	± 0.02	±.01	$\pm.01$	$\pm.01$	$\pm .02$	$\pm.02$	$\pm.02$
	GBC	0.56	0.56	0.55	0.66	0.66	0.65	0.67	0.67	0.67
-		± 0.02	± 0.01	± 0.01	$\pm .02$	$\pm.02$	$\pm.02$	$\pm .02$	$\pm.02$	$\pm.02$

Table 2: Performance of different algorithms todetect node ambiguity.

• Gini(n): sparsity index (David, 1968) of $\vec{W}(n)$.

3.1 Evaluation

Computing features. Topological features are efficiently extracted using the query tool mentioned in Section 2. To compute *textual features* (see Section 3) we use the *Glove* pre-trained word embedding vector (Pennington et al., 2014) of length 300 from the CommonCrawl.³

By combining these two types of features (topological and textual) we obtained three different vector input representations consisting of 6 (only topological features), 303 (only textual features) and 309 (textual and topological) dimensions respectively.

Finally, we created three "ground truth" sets of nodes in the graph for which $p_{SI}(n)$ is known. We selected a balanced number of monosemous and polysemous nouns, using the following sense inventories: i) WordNet (14,659 examples); ii) DBpedia (17,041 examples); iii) WordNet and DBpedia (31,701 examples).

Algorithms. We compared four algorithms:

- Random (*Rnd*): a random baseline which randomly classifies the ambiguity of a node;
- Neural Network (*NN*): a neural network with Softmax activation function in the output layer and dropout (Srivastava et al., 2014);

³https://nlp.stanford.edu/projects/glove/.

	WordNet					DBJ	pedia	WordNet \cup DBpedia		
	Features	dCor	ρ	PI weight \pm std	dCor	ρ	PI weight \pm std	dCor	ρ	PI weight \pm std
topological	$cc_{G^{-+}}$	0.593	0.185	$0.0039 {\pm} 0.0001$	0.614	0.228	0.0628±0.0051	0.513	0.027	$0.0038 {\pm} 0.0008$
	$v_{G^{-+}}$	0.602	0.203	0.0022 ± 0.0003	0.597	0.194	0.0045 ± 0.0010	0.513	0.025	$0.0025 {\pm} 0.0003$
	$e_{G^{-+}}$	0.597	0.194	$0.0100 {\pm} 0.0016$	0.600	0.200	$0.0048 {\pm} 0.0008$	0.514	0.027	$0.0024{\pm}0.0001$
	$cc_{G^{+-}}$	0.606	0.212	$0.0131 {\pm} 0.0013$	0.579	0.159	0.0092 ± 0.0016	0.492	-0.014	$0.0049 {\pm} 0.0003$
	$v_{G^{+-}}$	0.623	0.247	$0.0383{\pm}0.0035$	0.580	0.159	0.0029 ± 0.0009	0.495	-0.010	$0.0013 {\pm} 0.0008$
	$e_{G^{+-}}$	0.619	0.237	$0.0074{\pm}0.0010$	0.583	0.167	0.0034 ± 0.0013	0.497	-0.006	$0.0054{\pm}0.0004$
textual	Δ_{in}	0.379	-0.242	0.0699±0.0036	0.399	-0.202	0.0231 ± 0.0023	0.433	-0.134	0.0470±0.0027
	Δ_{out}	0.400	-0.199	$0.0101 {\pm} 0.0004$	0.415	-0.170	0.0037 ± 0.0015	0.431	-0.138	$0.0120 {\pm} 0.0007$
	Gini	0.443	-0.114	$0.0042 {\pm} 0.0004$	0.460	-0.080	0.0035 ± 0.0009	0.494	-0.013	$0.0059 {\pm} 0.0006$
	$\vec{W}(300 \text{ dimensions})$		Avg	$0.0029 {\pm} 0.0004$		Avg.	$0.0030 {\pm} 0.0005$		Avg	$0.0028 {\pm} 0.0003$
			Min	$0.0016 {\pm} 0.0003$		Min	0.0005 ± 0.0005		Min	$0.0014{\pm}0.0003$
			Max	$0.0077 {\pm} 0.0009$		Max	$0.0180 {\pm} 0.0013$		Max	$0.0123 {\pm} 0.0011$

Table 3: Distance correlation dCor and Pearson coefficient ρ between polysemy and features and Permutation Importance (PI) weights (NN estimator).

• Two ensemble-based learning algorithms, namely AdaBoost (*ABC*) (Zhu et al., 2009) and Gradient Boosting (*GBC*) (Friedman, 2001): both have been shown to have high predictive accuracy (Kotsiantis et al., 2006) and are good competitors of neural methods, especially with very large datasets.

Parameter selection. Based on the Area Under Curve ROC (AUC) analysis (Kim et al., 2017), *NN* parameters have been empirically set as follows: i) when testing only with topological features (6 dimensions), we use 2 hidden layers with 4 and 2 neurons respectively and a dropout of 0.2 and 0.15; ii) when using only textual (303 dimensions), or combined textual and topological features (309 dimensions), we use 4 hidden layers, with 128, 64, 32 and 8 neurons respectively and a dropout of 0.3,0.25,0.2 and 0.15.

Results. We show in Table 2 the resulting precision, recall and F_1 of the five systems across the ground truths datasets and for the combinations of features (see Section 3). The metrics are averaged on five classification experiments, with a random split (85% train, 10% validation and 5% test) of the ground truth sets. As shown in Table 2, *NN* outperforms the others ensemble methods, obtaining a F_1 score around 0.70. The comparison of performances across the three combinations of features reveals that topological features are not enough to build a model for polysemy classification but can slightly boost the overall already compelling performances of word embeddings-based features.

In Table 3 we show the Person coefficient ρ and

the distance correlation $dCor^4$, with the aim of analyzing how each feature correlates with the polysemy observed in the three ground truth dictionaries. We observed that the features with the highest correlation with polysemy are $e_{G^{+-}}$, $cc_{G^{-+}}$ and $v_{G^{-+}}$ (see Section 3). Additionally we report the resulting weights of Permutation Importance (PI) applied to the NN system with the aim of measuring how the performance decreases when a feature is perturbed, by shuffling its values across training examples (Breiman, 2001). We observed that the features which most influenced the performances are $\Delta_{in}(n)$ (WordNet and WordNet \cup DBpedia) and $cc_{G^{-+}}$ (DBpedia). Furthermore, we found that although topological features affect the performance only by a 1% in the average, a number of topologically related features, such as $cc_{G^{-+}}$, $v_{G^{-+}}$ and $e_{G^{+-}}$ are shown to be indeed related with polysemy. In our future work, we plan to create an ad-hoc groundtruth sense dictionary, since especially WordNet includes extremely fine-grained senses that do not help validating our conjecture about reduced mutual connectivity and contextual similarity of a node's neighborhood in case of monosemy.

4 Conclusion

The main contribution of this work is a new resource obtained by converting a large dataset of *is-a* (hypernymy) relations automatically extracted from the Web (such as WebIsADb) into a graph structure. This graph, along with its accompanying search tools, enables descriptive and predictive analytics of emerging properties of termino-

 $^{{}^4\}rho$ and dCor are indexes to estimate how two distributions are independent.

logical nodes. We used here our new resource to investigate whether a node *polysemy* can be predicted from its topological features (i.e., connectivity patterns) and textual features (meaning representations from word embeddings). The results of this preliminary study have shown that textual features are good predictors of polysemy, while topological features appear to be weaker predictors even if they have a significant correlation with the polysemy of the related node.

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