# Nonlinear Causality Inference in Microarray Time Series

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**Abstract.** Detecting causal relationships between time series data has been widely studied in many areas. One of the most popular causality inference methods is Granger causality that is a linear regression-based model for determining whether a single time series is useful in forecasting another; however, this approach cannot detect nonlinear relations in the data. In this work, we use Elastic-net regularization to infer linear Granger causalities in gene expression data. Moreover, we have proposed a method which uses the properties of kernel algorithms to infer nonlinear causalities.

**Keywords:** Causality inference · Granger causality · Gene regulatory networks

### 1 Introduction

Granger causality is a strong method for inferring causal relations among a number of time series data. According to the definition, if past values of X and Y together can predict future value of Y better that past values of Y alone, then time series X Granger-cause time series Y. One of the advantages of using Granger causality is to infer causal networks like gene regulatory networks (GRNs) from microarray time series data [1,5,3]. Real biological data sets have a problem which is about the big numbers of genes while we have few time steps  $(n \gg T)$ . Due to this problem, directly applying Granger causality is not feasible. In this work, we use Elastic-net regularization [6] which has the sparsity feature and can be applied to high dimensional settings.

Moreover, in GRNs, genes inherently have nonlinear intersections with each other; however, Granger causality is a linear method which is not capable of inferring the nonlinear interactions. For nonlinear dynamics of the time series data, different extensions of Granger causality have been proposed [4, 2].

Using Elastic-net regularization, the problem of high dimensional data has been already solved; however, to infer nonlinear interactions, we need to apply a more flexible method. As a result, we propose to use kernelized Elastic-net approach which uses the properties of kernel algorithms to infer nonlinear causalities.

### 2 Experiments

We use Human Cancer Cell Line (HeLa) dataset for evaluation. Here, we use experiment 3 which has more than 1100 genes and 48 time points.

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In Figure 1, we present a comparison between the two proposed methods, Elastic-net, and kernelized Elastic-net Granger causality.

The proposed method is capable of providing superior results in many cases. More specifically, kernelized Elastic-net provides high precision in the dataset.

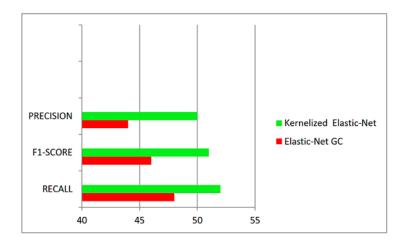


Fig. 1. Comparison between Elastic-net GC and kernelized Elastic-net GC

#### 3 Conclusion

Inferring causal relations could lead to gene regulatory networks; however, in microarray time series the number of genes is far more than the number of time points. We have used Elastic-net regularization to have both sparse and smooth solutions. We have also proposed a method which can be applied to infer nonlinear interaction in high dimensional settings.

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