Causation: revisited

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Abstract. From the standpoint of applied ontology, the problem of understanding and modeling causation has been recently challenged on the premise that causation is real. As a consequence, the following three results were obtained: (1) causation can be understood via the notion of systemic function; (2) any cause can be decomposed using only four subfunctions, namely *Achieves, Prevents, Allows* and *Disallows*; and (3) all these subfunctions can be defined in terms of *Achieves* alone. It follows that the essence of causation lies in a single function, namely *Achieves*.

It remains to elucidate the nature of the *Achieves* function, which has been elaborated only partially in the previous work. In this paper, we first discuss a couple of fundamental policies in the above mentioned causation theory since these are useful in the discussion, then summarize the results obtained in the former paper, and finally reveal the nature of *Achieves* giving a complete solution to the problem of what causation is.

Keywords. Causation, systemic function, device ontology, direct causation, state-mediation

1. Introduction

Although what causation is has been discussed for many years, it has been considered an unsolved problem to date. Assuming causation is real, this paper discusses causation as an occurrent (causing) and aims to demonstrate that it is essentially achieving. This view has been presented in [1] where the authors obtained the following results: (1) causation can be understood as a case of systemic function, and hence it is possible to talk about causation in terms of function, (2) Causing can be decomposed along two dimensions, direct/indirect and positive/negative, into the four subfunctions *Achieves*, *Prevents*, *Allows* and *Disallows*, and (3) *Prevents*, *Allows* and *Disallows* can be defined in terms of the *Achieves* function. It follows that causation is essentially understood in terms of *Achieves*.

The main goal of this paper is to uncover what *Achieves* is. This issue has been only partially tackled in [1]. Before addressing the main topic, the paper reviews how an occurrent causes another. This review leads to fruitful discussions of causation which relies on three policies adopted in the theory: (1) the state-centric approach, (2) the distinction between direct and indirect causations, and (3) the impossibility of direct causation between events. On the basis of these discussions and policies, we see why the conventional attempts to explain causality have not been successful. Then, after summarizing the results obtained in [1], we will turn to our main goal, the elucidation of the *Achieves* function. More precisely, we will reveal the nature of *Achieves* for all possible relata giving in this way a solution to the question of what causation is.

2. Presuppositions, Negative causation, and Fundamental claims

2.1 Typical existing theories

The main questions driving this research can be articulated as follows:

- (i) What is causation?
- (ii) Does a theory of causation explain (exclude) the known positive (negative) examples?

Typical attempts to define the causation $C \rightarrow E$ are listed below [2]:

- (1) E-type events regularly follow C-type events.
- (2) E is counterfactually dependent on C.
- (3) There is a spatiotemporally continuous transfer of energy or momentum from C to E.
- (4) C raises the probability of E.
- (5) By manipulating C, we could bring about changes in E.
- (6) Dispositional account of causation [3][4].

Unfortunately, it has been shown that none of these successfully answers the above questions[2][5].

2.2 Presuppositions

The view in this paper embraces the following five views and restrictions which were introduced and motivated in [1]. Note here that they are introduced for scoping the research.

Presupposition 1: Causation is real and not a mere cognitive artifact necessary for human understanding of phenomena.

Presupposition 2: We do not discuss epistemological causation. That is, identification of the cause of a given effect and prediction of the effects of a given cause are out of scope.

Presupposition 3: Human factors are out of scope. For example, we do not discuss causations such as "The cause of the accident is carelessness of the driver".

Presupposition 4: We only deal with phenomena in classical physics, and we assume causal relation is asymmetric, that is, if $C_1 \rightarrow E_1$, (read: C and E are events and C causes E), then $E_1 \rightarrow C_1$ does not hold.

Presupposition 5: We only discuss token-level causations. That is, we do not discuss causation like "Smoking causes cancer" but discuss what the "cause" is in "Tom's smoking caused him to contract cancer".

2.3 Negative causation

Generally speaking, negative causation is considered particularly challenging. It is known that there are two types of negative causation: causation of absence and causation by absence. An example of the former is

"No robbery occurred because John locked the door", and an example of the latter is "A thief broke into Tom's house because he did not lock the door."

Causations related to absent occurrences are common in daily life, and hence causal theories that cannot explain them fail at least at the practical level. That said, it is difficult to talk about non-existing entities even in applied ontological systems, in particular those developed within a realist approach. Resolving this problem is a challenging task. The theory discussed

in [1] can explain negative causation and overcome other disadvantages introduced in traditional approaches like, for instance, counterfactual theory [6].

2.4 Fundamental claims

Let us consider two examples: (a) Traffic accident and (b) Blood clot growth (See Fig. 3).

- al. A car hit a person.
- a2. A witness informed a fires station (EMS) of the accident.
- a3. An ambulance came and transferred the victim to a hospital.
- a4. The victim arrived at the hospital.
- a5. A doctor examined the victim.
- a6. etc.

- b1. A blood clot grew.
- b2. The blood vessel narrowed.
- b3. The flow rate of the blood reduced.
- b4. An organ downstream was lacking oxygen.
- b5. It contracted an ischemic disease
- b6. etc.

In spite of the difference of the domain, these two are often considered similar in terms of causation because, so the argument goes, the causal chains they manifest are similar. However a closer investigation reveals that they are very different from each other. What exists in the traffic accident is a sequence of completed processes (events). Each event happens after the former event has completed. On the other hand, at least the first three occurrents in the blood clot case happen concurrently, that is, it is wrong to say that the effective cross section of the blood vessel starts to decrease after the completion of the growth of the blood clot. This is a continuous and concurrent process with the decreasing in flow rate happening together with the clot growing. The occurrents in the case of the traffic accident have no direct interaction between them but interact with each other indirectly with the mediation of states, while there is no state-mediation in the case of blood clot and all the processes are ongoing after the organism downstream has contracted an ischemic disease.

The issue here is whether the causal interaction between two processes is done by mediation of state or not. Therefore, the fact that these processes are constituted of states is irrelevant here. In fact, direct interaction between two processes are mainly done by equation-based parameter propagation where no state-mediation exists between them (See 5.1).

Note here that such ischemic disease will not be cured even if the growth of the clot has terminated, since it has been caused by the state of the smaller cross section of the blood vessel rather than the growth process itself. This fact tells us a very important message which is summarized as:

Claim 1: States play crucial roles in causation. So, states necessarily appear in the relata of causation.

Although all the interactions between the occurrents in the traffic accident happen with the mediation of states, those between b1, b2 and b3 in the blood clot case happen directly on each other, and hence they do not need any state in between the causal interaction to occur. This fact suggests a new distinction among causation kinds:

Claim 2: There are two types of causation: *direct causation* and *indirect causation*. The latter happens with the mediation of states, while the former needs no state-mediation in between.

Imagine two occurrents causally connected to each other. In the terminology of [7], if they overlap, then the interaction between them must be of the type holding between processes rather than between events. Remember that any event, a completed process in [7], must be dealt with as a whole. This inherent property of an event prohibits direct interaction between

events. This is obvious from no completed occurrents can directly influence another one after the completion. These observations lead to our third claim:

Claim 3: There is no direct causation between events (understood as completed processes).

These three claims challenge the traditional view of causation as found in the literature. The state-based approach to causation is the basis for the theory of causation discussed in this paper as we are going to see in the next section.

3. Fundamental issues for fruitful discussion on causation

In this section, we discuss two fundamental issues derived from the above three claims for better discussion on causation.

3.1 How an occurrent causes another

Suppose that two causally connected events/processes C and E occurred consecutively (in turn) in which C has influenced E in some way. Such an influence must be a kind of interaction between C and E. As to the question of when/where it happens, only the following four sequences are logically possible:

- (a) C; the interaction; E
- (b) C(including the interaction); E
- (c) C; (including the interaction)E
- (d) C(including the interaction); (including the interaction)E

The first case seems not possible because the interaction between C and E cannot happen at the time in which C had completed and E has not happened yet. Therefore, an answer can be provided only by the other three cases. The essence of these three is that the interaction between C and E are included in either C or E. Considering that any interaction requires the participation of the interacting entities, here C and E, it turns out that only (d) where C and E are overlapped is valid. This conclusion coincides with our claims discussed earlier. That is, the fact that the case (a) does not hold corresponds to Claim 3: "There is no direct causation between events",. Case (d) corresponds the Claim 5 which will be introduced in section 5 and corresponds to: "Causal efficacy inheres in an event". Up to here, by interaction, we mean direct causation between processes or events. However, the case (a) turns out to be possible if we expand it to accept indirect interactions via states suggested by Claim 2. Some people might think an interaction, call it F, between C and E can be an ordinary process/event that mediates the influence of C on E. However, such thought fails under a regression argument because the same problem arises between C and F. Now let us consider the case where C and E meet (share the end and beginning instants). Direct causation is positive so that a substantial interaction like energy or momentum transfer should happen for C to influence E. However, such transfer cannot happen in an instant time because there is no instant occurrent in reality. Therefore, (d) is valid only for overlapping cases.

In summary, (a) is possible only in the case of indirect causation mediated by states created by C, while only (d) is possible if we confine the discussion to direct causation. In other words, the secret of how an occurrent causes another is hidden in the case (d) which we are going to discuss in section 5.2. As far as the author knows, none of the existing theories on causation including the six theories presented in 2.1 cares about the directedness of causation.

In the discussion on causation in the literature, not enough attention has been paid to the granularity of the occurrents and of the causal chain. In "John contracted cancer (E) because of smoking (C)", for example, a long causal chain is hidden between C and E, and hence these two events are not adjacent to each other in the causal chain. Special attention must be paid on the adjacency between the cause and its effect when discussing causation. Imagine, for example, a case where a discussion on the nature of $C \rightarrow E$ is made in a causal sequence which, when better detailed, turns out to be $C \rightarrow C^1 \rightarrow C^2 \rightarrow C^3 \rightarrow E$. The discussion would be problematic because it is not clear which causation is actually discussed. Is it the causation $C \rightarrow C^1$ or $C^1 \rightarrow C^2$, or else? Indeed, it is unclear what one means by the causation $C \rightarrow E$ where C and E are not adjacent in the first place. Some might express objections by saying that it is theoretically difficult to talk about adjacency of causal occurrents because finergrained causal sequences could exist between any causal pairs of events. Although the worry makes sense in many cases, it is not always true in reality. For example, "John kicked a ball (C) and it traveled away (E)" is a case where the cause and its effect are adjacent independently of the granularity. A kicking which is an impact-giving occurrent on an object by swinging one's leg is a complex of multiple micro motions, so it has a long causal sequence in it, but a kicking is a macro occurrent and refers to the entire sequence and hence the adjacency between the kicking and traveling occurrents remains unchanged. Concretely put, assume that a kicking (C) is composed of three finer causal units (say, $C^0 \to C^1 \to C^2 \to C^3$). Then the whole causal sequence becomes $C^0 \rightarrow C^1 \rightarrow C^2 \rightarrow C^3 \rightarrow E$ in which the last event before E (the ball's traveling) is \hat{C}^3 , i.e., the collision between the foot and the ball. There is no finergrained causal chains between C and E because C includes all events just before E happens. As described above, the kicking is thus a macro occurrent C that starts at C^0 and ends at C^3 . The reason why the adjacency is not influenced in this example is because what can be decomposed by introducing finer-granular causation is only the causal occurrent itself rather than the causal link (\rightarrow) . The boundary between the cause and its effect under consideration remains unchanged in the case of decomposition of occurrents.

Another popular example: "John struck a match (C) and the match fired (E)", is also inappropriate for fruitful discussion of the nature of causation. There are several important causal occurrents between C and E, for example: "John struck a match (C) \rightarrow frictional heat was generated \rightarrow the gunpowder ignited \rightarrow the match bar temperature rose \rightarrow the match bar fired (E)". Because of the existence of such a finer causal chain in between, it is not appropriate to argue about the causal relation between C and E without a theory of composition of a causal chain.

The important issues about adjacency can be summarized as follows:

- (1) Discussion of the nature of *causing* (denoted by \rightarrow) using examples (C \rightarrow E) must be done in the situation where the causal link being discussed is uniquely identified.
- (2) In order to uncover the nature of causation, we should first tackle the adjacent causation before the nature of causal chains.
- (3) Our new finding on directedness of causation is of importance because it is compliant with (1). Any direct causation has its unique "causing(→)" in C→E and problematic issues appear only in indirect causations.
- (4) Direct causations are unaffected by additive/subtractive interventions because, in the case of <Event → State> pattern, when the happening of the effect (E) is under consideration, the causal event (C) has completed already which guarantees E has happened, and in the case of <Process → Process>, as is discussed in 5.2.2, both C and

E are happening concurrently and hence at the time E exists C is necessarily happening. That is, there is no way to separate them. Needless to say, if C does not happen, there is no need to talk about E's occurrence. (In the case of indirect causation and/or a long causal chain, however, an intervention could occur at any time after C has completed) None of the six existing theories shown in 2.1 cares about the adjacency of causation.

4. Summary of the theory of causation

This section summarizes the achievements obtained in [1], which will be extended in section 5 to complete a presentation of the entire theory. First of all, we present informal definitions of state, process and event.

A process is an ongoing/progressive occurrent which exists at any instant as a whole while it is activated. It constitutes an event when completion.

An event is a completed occurrent and is dealt with as a whole spreading over the entire interval. It has temporal parts. While it cannot change, a process can. A sequence of events forms a process.

A state is a time-indexed quality and its consecutive change constitutes a process. While the quality inheres in the bearer, it (the bearer) participates in the state when viewed from temporal perspective.

4.1 Causation and function

Given a causation $C \rightarrow E$, an entity A composed of all entities participating in C can be said to perform a systemic function (see [8]) that achieves E by behaving in a certain way in C. Indeed, considering E as a systemic goal for C, we obtain the following claim:

Claim 4: Any causation can be mapped to a systemic function.

Technically, the validity of Claim 4 relies on a series of results that led to the introduction of notions like systemic context and systemic function [8], and theories like the device ontology [9]. The device ontology is a system of roles that generalizes an entity that acts as a device in the propagation of other entities (e.g., the heart as a device in a human body), and enables us to talk about behaviors of an entity in a system and of externally detectable input/output characteristics. The modeling is granularity-independent thanks to the recursive application to behavioral analysis of the components where necessary. Although we will briefly explain it in 5.1, readers can find the details of the device ontology in [1] and [9].

4.2 Essentials of causation

Note first that Claim 4 does not have a revisionist goal, it does not attempt to free the world from causation. The mapping instead aims to shed light on causation by studying it in terms of functions. In other words, while causation is assumed to be a truly ontological notion (Presupposition 1), its rewriting in terms of function helps to deepening its understanding. Of course, there is an obvious circularity in the causation-function mapping due to the fact that causation inheres in function. However, this circularity does not raise a problem here since there is no attempt to reduce the former to the latter. On the contrary, since the circularity makes evident the strict dependence of function over causation and since we already have a well-developed theory of function, it is interesting to see what we can learn by analyzing causality in terms of functions. The core of a function is the achievement of a goal by a behavior, which suggests that the most generic function is the *Achieve* function as we are

going to show.

4.3 The functional square

As stated earlier, there are two distinctions about causation: direct/indirect and positive/negative. Achieves is direct and positive. According to these two dimensions, there are four types of functions, see Table 1, with Achieves being classified as direct and positive. Achieves is investigated in section 5, here we

define the other three.

| ne the other three. | Table 1 | Functional square. | |
|--|---------|--------------------|-------|
| ments is defined as follows (for details see | | positive | negat |

ative *Prevents* is defined as follows (for details see direct Achieves Prevents Disallows indirect Allows

Definition 1 (Prevents): In context C, an occurrent X prevents an occurrent Y if and

only if there exists an occurrent Z in C such that (i) X Achieves Z in C, and (ii) Y and Z are incompatible in C by which we mean either Y or Z is true but not both in C.

Some readers may find it uncomfortable to bring up context when discussing causation, but this is by no means a relativization of causation to context, rather the opposite. It is by selecting a causation that automatically one also determines a context in which the causation holds. Imagine, for example, that "John could not enter the room because the door was locked". In order to make this causation valid, a context is required to ensure that there is no other way to enter the room (e.g., there is no other unlocked door or window) and he is not allowed to break in. Causal talks in the literature implicitly assume the existence of such contexts.

4.4 Indirect causation and preconditions

Many of the examples discussed thus far in the literature are examples of indirect causation as shown below.

Example 1: No robbery occurred because John locked the door.

Example 2: A thief broke into Tom's house because he did not lock the door.

Example 3: Emily's dog was bitten by an insect, contracting an eye disease as a result. Ignoring this, she did not take the dog to any animal hospital. Later the dog lost its sight. (extracted from [10]).

Example 4: A father pushing his child out of the way of a speeding car saved the child's life (i.e. causes it not to die). [11].

Example 5: The failure of delivering a piece of machinery in time caused a machine to break down.[12]

Nevertheless, the discussion of causation in the literature has been based on one type of causation "An occurrent C caused an occurrent E" without distinguishing between direct and indirect causation [2][5]. The proposal of the author is to adopt a state-centered view and to conceptualize indirect causation as state-mediated causation. From [1] we know that the result is significant. Taking this approach in combination with the functional view, one can show that many examples discussed in the literature are not about the Achieve function, but they are about the *Allow* and *Disallow* functions.

4.4.1 Preconditions

A precondition for an occurrent is a condition whose truth value influences the activation of the associated occurrent. Before defining the latter two functions, we note that there are two types of preconditions for an occurrent. We call one the *facilitative* precondition and the other the *preventive* precondition. Either one can be stated as follows:

Facilitative precondition for X:

If occurrent X occurs in context C, the facilitative precondition of X is true in C.

Preventive precondition for X:

If occurrent X occurs in context C, the preventive precondition of X is false in C.

4.4.2 Allows and Disallows

We can now define the functions Allows and Disallows.

Definition 2 (*Allows***)**: Occurrent X *Allows* occurrent Y in context C if and only if there is a state Z that satisfies one of the following conditions: In C, (i) X *Achieves* Z and Z is a facilitative precondition for Y, (ii) X *Prevents* Z and Z is a preventive precondition for Y, and (iii) X maintains Z and Z is a facilitative precondition for Y.

Definition 3 (*Disallows*): Occurrent X *Disallows* occurrent Y in context C if and only if there is a state Z that satisfies one of the following conditions: In C, (i) X *Achieves* Z and Z is a preventive precondition for Y, (ii) X *Prevents* Z and Z is a facilitative precondition for Y, and (iii) X maintains Z and Z is a preventive precondition for Y.

Note that the last two definitions use the function *Maintain* which originally refers to the function of outputting the incoming operand without changing it. The prototypical example is a conduit that outputs exactly what is fed into it: a water pipe has an output flow rate that is equal to the input flow rate. The general *Maintain* function performs similarly by keeping the current state unchanged. In terms of *Maintain*, "John did not lock the door" is paraphrased as he *Maintained* the lock in the unlocked state. In other words, the omission of an event that should have occurred *Maintains* the current state (by doing nothing). The introduction of *Maintain* thus overcomes the theoretical difficulty of mentioning an occurrent which does not happen.

5. On the Achieve function

The discussion we have done thus far enables us to confine the study of the meaning of causation to that of *Achieves*, and hence we need to investigate this function to shed light on what *causing* is. This section is devoted for this purpose.

5.1 Rule of how to apply the device ontology

The device ontology [9] is a system of roles such as *device (actor)*, *conduit*, *operand* and *medium* for capturing dynamic systems in a consistent manner. A device receives *operand* carried by *medium* and processes it to output. It has a nested structure for finer-granular phenomena. It is used to define function in a systemic context in which its input-output behavior realized by the internal processing plays the functional role under consideration in the given systemic context [8]. Assume a causation $C \to E$ is given. Considering E is a systemic goal achieved by the occurrent C, an entity composed of all objects participating in C can be said that it performs a systemic function that achieves E using C in that context.

This conceptual framework is elaborated in terms of "what to achieve" and "how to achieve" defined in function decomposition proposed in [13]. Then, we have the following: "what to achieve" corresponds to E and "how to achieve" to C, which shows a causal sequence of $C \rightarrow E$ is equivalent to *Achieves* function performed by the device identified by the above way. The implication of this device ontology-based modeling is significant. The key idea is to consider C in $C \rightarrow E$ an internal phenomena (occurrent) happening in a device which performs *Achieves* function. It contrasts the ordinary notion of a causal chain which is conceptualized

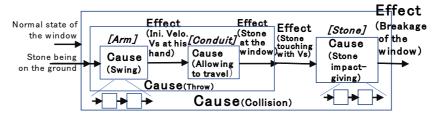


Fig. 1 Configuration of the window-breaking system, in which all inputs and outputs are states and all that are written headed by "Cause" in the box are events. In the finer granularity, some causation are of type Process => Process such as arm-swinging => stone-flying. The releasing event is omitted.

as a sequence of causally connected occurrents at the same level. On the other hand, our modeling is nested in multiple devices of different granularity in such a way that a cause is one-level deeper than the corresponding effect as is depicted in Fig. 1. Thanks to the granularity-free characteristic, the above way of application of device ontology to modeling of causation works for any causal pair of occurrents.

For example, suppose a situation where Tom threw a stone to the window of a house and it was broken because the stone hit it. Before the stone-throwing event, it seems there is no system which has a systemic function there. Tom, the stone and the window seem to exist independently of each other without forming any system and such a system does not have to be there. However, a system emerges when he has thrown a stone to the window. That is, whenever and wherever C→E exists a system is there because of the identification of a causation which reveals a certain connection between participants of the related occurrents. At the time when Tom held a stone and started to throw it to the window, his arm/hand, the stone and the window virtually form a system (device) in which three behaviors (occurrents) happen in turn: throwing motion, stone traveling and the stone hitting the window. Whether or not Tom has an intention to break the window does not matter here. Once a causation "Tom threw a stone to the window of a house and it was broken" is picked out, we can talk about a window breaking system composed of Tom's arm/hand and the stone together with a window as a target object. There would be three-level granularity. The coarsest granularity suggests to model the phenomena as a system (device) composed of the stone and his arm whose input is the normal state of the window and output is the breakage of the window caused by the collision, in which all the three occurrents are included (See Fig. 1). What happened in this system is analyzed in the second coarsest granularity. That is, two subsystems are identified: (1) the stone as a window-hitting subsystem and (2) his arm and a virtual conduit (the 3D region occupied by the trajectory of the stone) with the stone as a stone-travelling subsystem. In the first subsystem, the stone touching (hitting) the window with velocity Vs corresponds to the cause and the breakage of the window to the resultant occurrent (effect). The second subsystem models how the stone touches the window with Vs with input of the initial location (ground) of the stone and output of the final location (at the window) with Vs. The resulting configuration of system/subsystems is shown in Fig. 1. We now obtain a rule for the application of the device ontology in causation as occurrent:

[Rule] Identify a device by assigning E as output (what to achieve) and C as the internal behavior (how to achieve). If necessary, apply this rule to C recursively (e.g., in the case where C is a causal chain made of finer-granular occurrents).

5.2 The essentials of Achieves

Finally, it is time to investigate the *Achieves* function in all cases of relata in terms of the possible types such as event, process and state.

5.2.1 Event \rightarrow Process

A typical example is a collision of two balls in a billiard game. Imagine that a rolling white ball collides with a red ball at rest with velocity Va, and the red ball rolls afterwards. At first glance, it seems that the collision event causes the red ball rolling, but this is not accurate. There is no instant event in reality and any collision is a quick push process with a large acceleration. Because it is incorrect to say that the red ball starts rolling after collision, this should be <Process → Process> causation rather than <Event → Process>. In addition, what is activated by the collision is not an event but a process. Although some people might think the red ball rolling must begin by a starting event, but such a starting event is essentially a sub-event associated with all occurrents, it cannot be a relata of causation, since any relata must be an entity as a whole rather than a part. Another seemingly problematic example which seems to belong to the <Event → Process> pattern would be <A switch was turned on → the machine worked>. However, because what caused the machine to work is not the switch-turning behavior but the resulting "on" state of the switch, this is not a direct but an indirect causation. The above observation suggests that there is no <Event → Process> pattern in the real world. This is due to the nature of an event which must be dealt with as a whole at any time [7] and once it has terminated there is no way to influence others except via resultant intermediate states. However, such state-mediated causation is an indirect causation. If the causal influence happens before the termination, then it is not an event but a process which performs the influence as discussed in the next sub-section.

5.2.2 Process \rightarrow Process

A typical example of this pattern is a pair of a piston and a crank (see Fig. 2). The piston and the crank are connected to each other by a joint so that their behaviors (piston's downward and crank's rotation) are interlocked and are necessarily synchronized. In other words, the two processes happen concurrently which is the common interaction of this pattern. A remarkable feature of the $P \rightarrow P$ pattern is that its effect is generated via laws such as f=ma or law-like formula such as x=y which is free from causation. In the case of the push process of the piston & crank, for example, it seems that the piston exerts force f on the crank and the crank moves with acceleration a (= f/m). Although it would be correct in terms of Newtonian



Fig. 2 Pair of a piston and a crank.

mechanics, we try to avoid application of physical laws as much as possible because they are hypotheses in nature and they might unconsciously introduce hidden causation. Therefore, we concentrate on the fact that there exists a shared individual in any pushing/pulling phenomena caused by contact force. That is, we identify an equation x=y in which x and y are positions/speeds/accelerations of the bottom edge of the piston rod and the edge of the crank, respectively. We talk of these two behaviors (motions) without using formula f=ma. (The equation x=y is not a law but a causation-free formula which holds a priori and hence we can accept it as given truth.) This is why we introduce *equation-based*

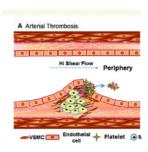


Fig. 3 Blood clot.

parameter propagation. A similar equation is found in the blood clot case shown in Fig. 3 in which x=y+z holds where x is the cross section of the blood vessel, y is the area of the vertical cross section of the clot and z the cross section of the effective channel of the blood vessel. This is also such a formula that we can accept as given truth rather than an equation derived from a physical law. A typical example of *Achieves* of this type is *throwing (an object)* as a process in which the position and velocity is shared by the hand and the object (x=y) and *Allows*, by releasing, the object to travel with the initial position and velocity at the time of the release. Other examples include *push*, *pull*, *warm*, *cool*, *etc*.

(a) Equation-based parameter propagation

The issue we need to discuss as to the causation in the pattern of $P \rightarrow P$ is whether the propagation through such formula is causal or not. Although y increases if x increases in the case of x=y, it happens not because of the relation between x and y is causal, since the reason why x=y holds in the case of the piston & crank is because both objects share the same entity (the joint) and there is only one motion of the same entity with two different perspectives. So, it seems there is no causation in the propagation made through x=y. However, there exist two phenomena in which the piston pushes down the crank and the crank pulls down the piston. These two phenomena are causally different, though the observable behaviors are the same. We need a more careful investigation into this.

We have neglected $\langle Process \rightarrow State \rangle$ as a pattern in the discussion because it is understood to be included in the pattern of $\langle Process \rightarrow Process \rangle$ because a process is a continuous/ consecutive change of states. Nevertheless, if we try to understand what is happening at each time instance during the interval when the process is ongoing, it is useful to investigate the $\langle Process \rightarrow State \rangle$ case. Similar to the discussion in the case of $\langle Event \rightarrow State \rangle$ discussed in 5.2.4 in which the state is obtained as the result of the completed event, the state on the right-hand side of $\langle Process \rightarrow State \rangle$ seems to be also the result of the process on the left-hand side. To support this conclusion we need to understand the state in the process and the propagation from the state on the left-hand side to that on the right-hand side. Note here that a process is a sequence of state change. In other words, a state or a set of states form a process when they change as time goes, and as a result, a new state keeps being created at any time while the process is ongoing. All processes can be said that they have causation in their state change. Let us examine this claim for the possible two cases:

[Case 1] In the case that the process under consideration has an operand (target object), the state change of the operand is the result of some operation done by the action/occurrent intrinsically specified in it. So, the state change of the object is causal.

[Case 2] In the case of no operand, that is, occurrents denoted by intransitive verbs, on the other hand, we need more neat consideration.

Let us take "growing" as an example. Growth of an organism is made thanks to a lot of internal biological activities of its parts. The result of the growth is of variety according to attributes/states we pay attention. When we concentrate on its size, we observe enlarging process of its size and it is a sequence of state change in terms of the size. Apparently, it is caused by those internal activities in the growth. Although walking is an action denoted by an intransitive verb walk, <John walking \rightarrow John's location changing> is causal because walking has a couple of complex internal causal occurrents inside which enables John to walk and his location change is its effect.

5.2.3 State \rightarrow State

We have discussed $\langle \text{Event} \rightarrow \text{Process} \rangle$, $\langle \text{Process} \rightarrow \text{Process} \rangle$ and $\langle \text{Process} \rightarrow \text{State} \rangle$ patterns. The next is the pattern $\langle \text{State} \rightarrow \text{State} \rangle$. The blood clot case shown in Fig. 3 is a typical example of this pattern which is analogous to a flow-control valve in fluid dynamics in which $\langle \text{The half-closed state of a valve} \rightarrow \text{The half flow rate} \rangle$ holds. In general, such a case where a state can be a cause of some occurrent is limited to the case where it is an internal state of a device. Needless to say, the growth of a blood clot is equivalent to dynamic generation of a flow-control valve (with closing behavior) in the blood vessel.

Causation we have discussed thus far is based on change which is characterized as the non-zero derivative and on its propagation. In particular, device ontology works mainly for such changes. Note here that there is another kind of change in the talk of causation. It is the deviation from the standard and examples are found in flow-control valve and the blood clot cases discussed above. We do not have a causal theory for such change yet. The causation < the half-closed state of a valve $(S1)^1 \rightarrow$ the half flow rate (S2) > is not based on the non-zero derivative changes and is a complex causal phenomena based on finer-grained causal occurrents. Although it seems difficult to tackle it at first glance, it is fairly easy to model it in terms of the combination of <Process \rightarrow State> together with the recursive application of device ontology based on the rule discussed in 5.1.

Let us take a flow-control valve as an example. Assume the valve has started to close and stopped at an intermediate state between full open and full closed. Let S1 be the valve opening state after the deviation from the full open state. The phenomena as a whole is an closing event E1 but $\langle E1 \rightarrow S1 \rangle$ is not valid because it is not causation but a description of a phenomenon from two different perspectives. Nevertheless, there are several internal phenomena which causes to increase the resistance against the smooth flow of the fluid and hence the flow rate is smaller than the standard (S2). To see what happens in terms of changes with non-zero derivative, we investigate it according to two cases: (i) valve's closing process P1 is ongoing and (ii) P1 has terminated to become valve's closing event E1. Following the theory in [7], E1 is constituted of P1. While P1 is ongoing, the valve closing process P1 causes increase of the resistance against the smooth flow of the fluid so that the flow-ratedecreasing process P2 is ongoing. Therefore, <P1 → P2> holds and at any time instance during the process is ongoing $\langle P1 \rightarrow S2 \rangle$ holds. On the other hand, when P1 has terminated, then $\langle E1 \rightarrow S2 \rangle$ is established and S2 is output. Considering S1 is also the state when E1 has terminated, the above observations suggest that the pattern $\langle S1 \rightarrow S2 \rangle$ does not mean propagation of changes but rather continuation of causal phenomena caused by an occurrent

¹ Hereafter, S1 and S2 denote not only the state "half-xyz" but also any state deviated from the standard value (state).

of other patterns, say, $\langle P1 \rightarrow P2 \rangle$. We do not have functions of this type other than Cause.

It would be worth to note the fact that both $\langle E1 \rightarrow S2 \rangle$ and $\langle P1 \rightarrow S2 \rangle$ hold in the case of flow-control valve is neither usual nor trivial. The continuity of the output state between an event and its constituent process does not always happen. Imagine a cutting process and the corresponding event. At any time the cutting process is ongoing, the object has not been separated yet. It has been separated only after the completion of the cutting event.

5.2.4 Event \rightarrow State

The last pattern is <Event → State>. Whenever an event has completed, a resulting state is generated and it lasts for a while. When you cut an object, it becomes separated. When you buy a good of 10 USD, then your pocket money decreases by that amount and you obtain the ownership of the good. When you finish your daily walk to the park, then you are back to your home again. In all cases, the corresponding resultant states are successfully realized or achieved when any event has completed. Note here that in such cases, no intervention would occur before getting the resulting state. This is because if the event has not completed, there is no need to talk about its effect. As we see thus far, this pattern nicely demonstrates that the essential of causation is generating a new resultant state which would eventually causes (Allows or Disallows) succeeding occurrents. Considering <Process → Process> and <State → State> patterns tend to work as continuation or maintaining of existing states and/or their change [14], <Event → State> pattern plays the key role in causation by creating a new state. As we have already seen thus far, there are many example functions of this type and *cut* is one of the most typical ones. Considering that most processes will have eventually terminated to constitute an event with resultant states, many of the concrete functions belong to this type such as kill, produce, inform, delete, transfer, etc.

5.3 How to terminate the recursive application of device ontology

In the above discussion, especially in the case of $\langle P \rightarrow P \rangle$, analysis of the internal causal phenomena is deferred to recursive application of device ontology to cope with finer-granular phenomena as indicated by the rule presented in 5.1 (See Fig. 1). Completion of our discussion on causation requires us to guarantee the recursive application will terminate without leaving any ambiguity of what *Achieves* is. This problem is resolved as follows.

Recursive application of the device ontology definitely terminates when it reaches the minimal granularity. So, we have the following two cases:

- (a) The change under consideration cannot be attributed to the inner causal phenomena of the device, and hence it is because of proactive phenomena such as Alpha collapse which are not reduced to more fundamental phenomena.
- (b) Except (a) there are only two cases: either $\langle E1 \rightarrow S2 \rangle$ or $\langle P1 \rightarrow P2/S2 \rangle$. In either case, S2 has been obtained using a certain propagation of S1 causally obtained by E1 or P1.

The latter is apparently what we have discussed thus far so that we can identify causal source. Only the case (a) remains to be discussed. The issue is how many such principles that are irreducible to finer causal phenomena, exist and how much they influence our theory of causation. Although we cannot provide a proof, there seems to exist only a few such principles, which we introduce as primitives into our theory. We can summarize what we have discussed in the following three claims:

Claim 5: Causal efficacy inheres in each event as the pattern of <Event → State> rather than

between events. It is production of a new resultant state when an event has completed.

Claim 6: *Achieves,* which is the core subfunction of causation, is characterized by the three patterns: <Event → State>, <Process → Process> and <State → State>.

Claim 7: Any causation in reality is a sequence of occurrents connected by either one of the four subfunctions: *Achieves, Prevents, Allows* or *Disallows*.

We need to elaborate the role of *Allows* in causal chains. Informally put, it makes one of the facilitative preconditions of an occurrent true so that it literally allows the occurrent to happen, that is, the occurrent does not necessarily happen then and when it happens is undetermined. What is interesting, however, is in the case of no preventive preconditions, when an *Allows* happens to make the last false facilitative precondition true, the occurrent happens at the very time when *Allows* has happened. A typical example is a switch-turning event which is understood as an *Allows* for a machine to work by *Achieve*-ing the "on state" of the switch which must have been in the last false facilitative precondition of the machine to work.

6. Concluding remarks

We have discussed causation not as a relation but as an occurrent at the token level and claimed that *causing corresponds to achieving*. After presenting three main claims we discussed how an occurrent causes another together with the role of the notion of directedness of causation. Then, we gave a brief summary of the achievements obtained in [1]. We finally investigated the nature of the direct function Achieves, and showed that the source of causation inheres in an event and that the <Event \rightarrow State> and <Process \rightarrow Process> patterns play the key role in causation.

We have outlined a proposed theory of causation. The future work includes formalization of our theory and proper positioning of the theory in the rich history of causal theories including a closely related work [15] as well as a theory of causal chains. Apparently, such a causal chain that is composed only of *Achieves* would be equivalent with *Achieves* as a whole. However, many of the real causal chains would be composed of the four subfunctions: *Achieves, Prevents, Allows* and *Disallows*. We need a theory for explaining what causation a causal chain is as a whole in terms of these for subfunctions.

Finally, some implications of our findings are worth noting. Our theory is free from the simultaneity issues because it does not assume precedence of a cause to its effect. Thanks to its sole assumption of asymmetry, it can cope with it and arrange causal ordering consistently with the time flow from cause to effect. Another implication is the necessity of causation. It is apparent from the proposed four subfunctions that direct causation is necessary and the *Allow* function is not. Because most of real causations are causal chains which would include *Allows* subfunction, we can conclude they cannot be necessary. A rigorous definition of system and state, on which the theory relies, is still lacking. These are a genuine philosophical issues and hence go beyond the scope of this paper.

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