Extended Security Analysis of the Zaslavsky Maps Based Pseudorandom Byte Generator

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Abstract. The Zaslavsky maps based pseudorandom byte generator is a recent and secure cryptographic primitive. Extended security analysis of the generator is presented. We evaluated the output byte properties by period and linear complexity calculation and DieHarder and PractRand statistical packages. This gives the motivation to consider the Zaslavsky systems based pseudorandom byte generator as reasonable for basic cryptographic applications in encryption process.

Keywords: Zaslavsky Map, Pseudorandom Generator, Security Analysis.

1 Introduction

Cryptanalysis is the study of analyzing cipher text, ciphers and cryptographic primitives with the aim of understanding how they operate and finding and improving methods for defeating or destroying them. Pseudorandom byte generators are distinct algorithms that use mathematical formulas to output bytes with random like properties.

The use of chaos maps as a secure cryptographic system in the last thirty years has been at the prominence of dynamical equations. In [1], a new scheme for generating pseudorandom numbers based on Duffing map is presented. In [2], a security evaluation of the pseudorandom bit out algorithm based on multi-modal maps is proposed. Novel cryptanalysis of the number for video encryption is designed in [3]. In [4], a chaos game based pseudorandom number generator is presented. Number of pseudorandom bit output algorithms based on chaotic systems are designed in [5], [6], and [7].

Zaslavsky maps [8] based pseudorandom byte generator is presented in [9]. The generator is described in details, and the cryptographic analysis, including initial key evaluation and statistical analysis, is carried out.

The aim of the article is to present new analysis of some cryptographic properties of Zaslavsky maps based pseudorandom byte generator. In Section 2, the steps of the generator are described. Section 3 presents calculations of the period and the linear complexity, and DieHarder [10] and PractRand [11] statistical results are given. Finally, the last section concludes the article.

2 Description of the Zaslavsky Maps based Pseudorandom Byte Generator

The mathematical expression of the Zaslavsky equations is given by:

$$y_{n+1} = mod(y_n + v(1 + \mu z_n) + \varepsilon v \mu \cos(2\pi y_n), 1)$$
(1)

$$z_{n+1} = e^{-r} (z_n + \varepsilon \cos(2\pi y_n)) \tag{2}$$

where

$$\mu = 1 - e^{-r/r}, \tag{3}$$

r = 3.0, v = 400/3, and $\varepsilon = 0.3$. The generator under present study is based on two Zaslavsky chaotic systems. The initial parameters $y_{1,0}$, $y_{2,0}$, $z_{1,0}$, and $z_{2,0}$ are real numbers. With each iteration, four real values $y_{1,i}$, $y_{2,j}$, $z_{1,i}$, and $z_{2,j}$, are generated, then converted to 256 bit values, and XOR-ed. Pseudorandom byte *m* is outputted.

3 Extended Security Analysis of the Zaslavsky Maps based Pseudorandom Byte Generator

3.1 Period and Linear Complexity

The period and linear complexity of two hundred sequences of length M=200,000 of the generator were computed using SAGE [12]. The values obtained are comparable to those reported in [13]. Each tested binary sequence had huge period of M and linear complexity value of $(M/2)\pm 1$.

3.2 Experimental Testing with Statistical Packages

The DieHarder package (version 3.31.1) is a random number generator-testing suite. This testing and benchmarking software program consists tests presented in Table 1 *and* Table 2.

The DieHarder output results are presented in Table 1 and Table 2.

| Test name | p-value | Assessment |
|--------------------|------------|------------|
| diehard birthdays | 0.56483962 | passed |
| diehard operm5 | 0.26303032 | passed |
| diehard rank 32x32 | 0.52810343 | passed |

Table 1. DieHarder test results, I part.

| diehard rank 6x8 | 0.95957035 | passed |
|-------------------------|------------------------|--------|
| diehard bitstream | 0.53527613 | passed |
| diehard opso | 0.91909082 | passed |
| diehard oqso | 0.86167844 | passed |
| diehard dna | 0.93016479 | passed |
| diehard count 1s stream | 0.22990683 | passed |
| diehard parking lot | 0.88193571 | passed |
| diehard 2dsphere | 0.47770491 | passed |
| diehard 3dsphere | 0.97957902 | passed |
| diehard squeeze | 0.97235302 | passed |
| diehard sums | 0.02026052 | passed |
| diehard runs | 0.39874109, 0.90351885 | passed |
| diehard craps | 0.36983582, 0.86498446 | passed |

Table 2. DieHarder test results, II part.

| Test name | p-value | Assessment |
|----------------------|------------------------|------------|
| count the 1s byte | 0.24207567 | passed |
| marsaglia tsang gcd | 0.50132978, 0.67555797 | passed |
| sts monobit | 0.72146044 | passed |
| sts runs | 0.40218825 | passed |
| sts serial | 0.011460320.98601086 | passed |
| rgb bitdist | 0.011232230.95692540 | passed |
| rgb minimum distance | 0.119647880.90910943 | passed |
| rgb permutations | 0.370555710.96669890 | passed |
| rgb lagged sum | 0.084860530.97133190 | passed |
| rgb kstest test | 0.84077327 | passed |
| dab bytedistrib | 0.76852095 | passed |
| dab dct | 0.53079707 | passed |
| dab filltree | 0.22119502, 0.70442029 | passed |
| dab filltree2 | 0.90468519, 0.94557881 | passed |
| dab monobit2 | 0.94581666 | passed |

The second package is PractRand. We tested our pseudorandom scheme for bytes up to 2^{24} bytes in length, Table 3 *and* Table 4.

| Test name | Raw | Processed |
|----------------|---------|-----------|
| BCFN(2,13):! | R= +0.0 | "pass" |
| BCFN(2+0,13-3) | R= -0.6 | p = 0.588 |
| BCFN(2+1,13-4) | R= -2.2 | p = 0.814 |
| BCFN(2+2,13-5) | R= +1.9 | p = 0.202 |
| BCFN(2+3,13-5) | R= -0.3 | p = 0.526 |
| BCFN(2+4,13-6) | R= +1.6 | p = 0.236 |
| BCFN(2+5,13-6) | R= -2.5 | p = 0.860 |
| BCFN(2+6,13-7) | R= -3.0 | p = 0.921 |
| BCFN(2+7,13-8) | R= +5.0 | p = 0.033 |
| DC6-9x1Bytes-1 | R= +3.0 | p = 0.121 |

 Table 3. PractRand test results, I part.

 Table 4. PractRand test results, II part.

| Test name | Raw | Processed |
|------------------------|---------|-----------|
| Gap-16:! | R= +0.0 | "pass" |
| Gap-16:A | R= +2.1 | p = 0.147 |
| Gap-16:B | R= +0.8 | p = 0.284 |
| [Low1/8]BCFN(2,13):! | R= +0.0 | "pass" |
| [Low1/8]BCFN(2+0,13-5) | R= -2.3 | p = 0.829 |
| [Low1/8]BCFN(2+1,13-6) | R= -4.6 | p = 0.988 |
| [Low1/8]BCFN(2+2,13-6) | R= -1.3 | p = 0.683 |
| [Low1/8]BCFN(2+3,13-7) | R= -1.2 | p = 0.662 |
| [Low1/8]BCFN(2+4,13-8) | R= -0.2 | p = 0.468 |
| [Low1/8]DC6-9x1Bytes-1 | R= -1.3 | p = 0.829 |
| [Low1/8]Gap-16:! | R= +0.0 | "pass" |
| [Low1/8]Gap-16:A | R= +1.9 | p = 0.159 |
| [Low1/8]Gap-16:B | R= -0.5 | p = 0.634 |

The size of initial values can guarantee long period and good linear complexity of the output stream. All probability values, calculated from DieHarder and PractRand tests are in acceptable range of [0, 1). Based on these results we can conclude that all of statistical tests are passing successfully and the generator under present study is very suitable for critical cryptographic applications.

4 Conclusions

We have presented new security analysis of the Zaslavsky functions based pseudorandom byte generator. The results from the period, linear complexity, and DieHarder and PractRand statistical packages evaluation, indicate that the studied algorithm is reasonable for basic cryptographic applications in derivative encryption schemes.

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