# **Computer and Physical Modeling for Verification of the Stereo System Calibration Parameters Optimization Results**

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#### Abstract

Close-range photogrammetry is widely used to measure surface shapes and diagnose deformation. Usually, a stereo system of video cameras is used to register images of the measured object from several different angles. The surface shape is determined by triangulating a set of 2D points from these images. Triangulation uses the stereo system calibration parameters, which are determined before the experiment. Measurements during conditions with increased vibration loads can lead to a change in the relative position of the cameras of the stereo system (decalibration). This leads to a change in the actual calibration parameters and an increase in the measurement error. The decalibration problem can be solved using multidimensional optimization algorithms. To verify their calculation's results it is proposed to use a computer and physical modeling of decalibration of a video camera stereo system in laboratory conditions. The paper presents the implementation of the optimizing algorithm for the external parameters of a stereo system and the results of its performance during the experimental investigations.

#### **Keywords**

Close-range photogrammetry, stereo system decalibration, stereo system calibration parameters optimization, computer modeling, physical modeling

# 1. Introduction

Optical methods for measuring surface shape and deformations have many advantages over classical contact and strain gauge methods. The main advantage of optical methods is the ability to obtain results from a large area simultaneously, which allows you to get qualitatively better results during measurements. Photogrammetry [1] combines a large number of approaches to measuring three-dimensional spatial geometric parameters of objects based on the processing of two-dimensional images of these objects. Close-range photogrammetry [2] is used to measure parameters, including surface shape, of relatively small objects [3]. The main advantage of such methods is the ability to carry out non-contact measurements, including field experiments.

The main goal of photogrammetric methods is to find the position of spatial points with unknown three-dimensional coordinates. For this, it is necessary to find a pair of two-dimensional coordinates of these points in the two images that were recorded with two digital cameras. Further, the founded coordinates using triangulation according to the known internal and external parameters of the stereo system of video cameras give the desired three-dimensional coordinates of a point in space.

Several mathematical models are used to describe the transformation of three-dimensional coordinates into two-dimensional when registering images. One of the most popular in computer vision is the pinhole camera model. In it, the image is formed by projecting three-dimensional points on the image plane using a perspective transformation

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GraphiCon 2021: 31st International Conference on Computer Graphics and Vision, September 27-30, 2021, Nizhny Novgorod, Russia

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CEUR Workshop Proceedings (CEUR-WS.org)

$$s \begin{pmatrix} x_c \\ y_c \\ 1 \end{pmatrix} = \begin{pmatrix} f_x & 0 & c_x \\ 0 & f_y & c_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \end{pmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix},$$
(1)

where (X, Y, Z) is the three-dimensional coordinate of the point,  $(x_c, y_c)$  is the two-dimensional coordinate of the point on the image,  $r_{11}...r_{33}$  are the coefficients of the rotation matrix,  $t_x$ ,  $t_y$  and  $t_z$  are the coefficients of the transfer matrix,  $(c_x, c_y)$  are the coordinates the principal point (the point of intersection of the optical axis and the plane of the matrices),  $f_x$ ,  $f_y$  is the focal segment expressed in pixels, s is the scale factor arising from the use of homogeneous coordinates. The focal length of the optical system, the coordinates of the principal point, the coefficients of optical aberrations (internal parameters), and the coefficients of the transfer and rotation matrices (external parameters) are determined during the calibration procedure. This procedure is usually performed before or immediately after taking measurements.

Photogrammetric measurements can often be carried out during high vibration loads. Vibrations cause the cameras to move relative to each other during measurements. They lead to a change in both the external and the internal parameters of the stereo system. This process is called decalibration [4]. It leads to a noticeable increase in the measurement error.

Displacement of the cameras relative to each other can be corrected by carrying out the recalibration procedure, which consists of optimizing the parameters of the calibration matrix to minimize the triangulation error. That approach was already used in other works. In [5] recalibration for a system consisting of several cameras is described. External parameters are recalculated for a camera changing its position using information from cameras that remained motionless. In [6], according to a similar principle for the PIV stereo system, the position of the laser knife is corrected, but not the relative position of the cameras. In [7] for the PIV tomographic system, the mutual arrangement of the cameras is corrected, but a camera model is based on the polynomial function. In [4], the results of flight measurements of VUT100 Cobra aircraft wing deformations are presented. The presence of the stereo system decalibration effect during a flight increases the measurement error. Based on the experimental images, a recalibration procedure was carried out. It makes it possible to significantly reduce the triangulation error. The main disadvantage of this approach is the lack of verification of measurement results.

As in other works devoted to this issue, the decalibration problem is proposed to be solved using multidimensional optimization. When choosing a specific optimization algorithm, an analysis of existing methods was carried out [8]. To solve the problem, the Nelder-Mead algorithm was chosen [9]. This is the most well-known method among the non-directional strategy methods. The method is based on the fact that the experimental sample containing the smallest number of points is a simplex.

A regular simplex in an N-dimensional space is a polyhedron formed by N + 1 equidistant points the vertices of the simplex. An important property of the simplex is that a new simplex can be constructed on any face of the original one by reflecting a vertex relative to the center of gravity of all other vertices of the simplex.

Advantages of the Nelder-Mead algorithm are simplicity, a small number of preset parameters, a simple search strategy, calculating only function values, a small amount of memory required. Disadvantages of the method: the method works efficiently for  $N \le 6$ , the algorithm is based on cyclic motion along with coordinates. This can lead to the degeneration of the algorithm into an infinite sequence of exploratory searches without pattern matching.

#### 2. Computer modeling

The measurement error introduced by decalibration can be evaluated to estimate the possibility of optimizing the calibration parameters of a stereo system. For this, computer modeling was carried out. The decalibration modeling process is as follows:

1. the camera parameters are set, both internal (focal lengths, pixel size, and coordinates of the principal point) and external (vector of displacement and rotation of cameras relative to each other), all these parameters are determined in the experiment, at the stage of camera calibration;

2. the measurement object is formed as a set of points in 3-dimensional space;

3. without displacement (decalibration), by projecting 3D points onto the image plane of the cameras, 2D points are calculated, which act as actually received images from the cameras;

4. a known offset (decalibration) is set as the vector of displacement and/or rotation of the cameras relative to each other;

5. taking into account the changed external parameters of the cameras and the 2D points obtained in item 3, the 3D points of the object are calculated by triangulation;

6. then the obtained 3D points are again projected onto the image plane of the cameras, as a result of which we get reprojected 2D;

7. further, comparing the original 2D points and the reprojected ones, the magnitude of the reprojection error is estimated.

The following values were used in the computer modeling: the ratio of focus to pixel size is equal to 7500, the center point of the camera [1250, 980], displacement of one camera relative to the other  $T_x = -315$  mm,  $T_y = 115$  mm,  $T_z = 40$  mm, rotation of one camera relative to the another one around the x-axis is 3.5°, the y-axis is 12°, the z-axis is -1°. Parameters of the measured object: distance to the object is 1.5 m, object size is  $30 \times 20$  cm<sup>2</sup>, the number of points is  $10 \times 10$ , the angle of inclination of the coordinate reference system. These parameters were taken as an example of the actual calibration parameters of the stereo system and the measured object used in laboratory experiments.

Modeling showed that simple optimization by displacement or rotation by one axis will not lead to a global minimum of it, i.e. no correct or close to correct solution will be received. Therefore, in the optimization process, the objective function of the reprojection error depending on six parameters is minimized. The parameters are:  $T_x$ ,  $T_y$ ,  $T_z$  are the elements of the displacement vector, and  $\alpha$ ,  $\beta$ ,  $\gamma$  are the angles of rotation of one camera relative to the other. In step 4, the offsets are performed by the Nelder-Mead method, and then steps 5, 6, 7, etc. are repeated until we reach the maximum iteration value or the reprojection error value is less than the specified one.

An example of the dependence of reprojection error on displacement along the x-axis and rotation around the x-axis (with and without optimization) is shown in Figure 1. The vertical axis (mean square deviation (RMS) in pixels) is displayed in logarithmic scale, in red the result without optimization, and in green the result with optimization. Optimization was performed by the Nelder-Mead method in conjunction with the penalty function method. The number of attempts for each of the displacements is equal to 12, the maximum number of iterations in each attempt is equal to 500, the steps for calculating displacements are 0.1 mm and  $0.02^{\circ}$ .



**Figure 1**: Dependence of the reprojection error on bias without optimization (top) and with optimization (bottom)

It can be seen from the Figure 1 that the reprojection error as a result of optimization has significantly decreased, by about two orders of magnitude. It is not worth counting on the same error reduction in physical modeling, since the error of reprojection without displacements in real cases is much higher.

## 3. Physical modeling

For experimental verification of the optimization algorithm, an experimental setup was developed (see Figure 2). It is intended for physical modeling of the process of decalibration of a video camera stereo system. The decalibration is performed by moving one of the cameras using linear motorized movement modules controlled from a personal computer.

The movable camera is attached to a 3-axis positioner from Zaber. It consists of 3 separate X-LSM050A miniature motorized linear stages with built-in controllers with the following characteristics: travel range 50 mm, position error 20  $\mu$ m, and offset step less than 0.1 mm.

For experimental research, a test installation described in [10–11] was used. It allows to set a random three-dimensional surface and measure its profile using a laser distance sensor with an accuracy of 75  $\mu$ m. Two Basler piA2400-17gm cameras with the lenses Fujinon HF25HA-1B are used to register images. Cameras have a resolution of 2456×2058 pixels, and a pixel size of 3.45×3.45  $\mu$ m. The lenses have a focal length of 25 mm and an aperture ratio of 1:1.4.





**Figure 2**: Experimental setup: 1 - fixed camera; 2 - movable camera; 3 - 3-axis positioner; 4 - camera tripod; 5 - measurement object; 6 - laser distance sensor; 7 - 2-axis laser positioner; 8 - servos for deformation of the object surface; 9 - additional lighting



**Figure 3**: Dependences of the reprojection error on camera displacements: a – the first shape of the object surface; b – the second shape of the object's surface; c – the third shape of the object surface

In experimental studies, the Image Pattern Correlation Technique (IPCT) [12] was used to measure a three-dimensional surface. This optical method is based on cross-correlation image processing. A random pattern is preliminarily applied to the investigated surface, consisting of black dots on a white background. The corresponding coordinates of the surface points are determined with the help of the cross-correlation function. These coordinates then will be used in the triangulation process. This algorithm is widely used in optical methods for studying flows: Particle Image Velocimetry (PIV) and Background Orientied Schlieren (BOS) [13].

Graphs of the dependences of the reprojection error on the displacement of one camera relative to the other were built. The optimization of the external parameters of the cameras to reduce the reprojection error was performed. In Figure 3, solid lines indicate reprojection errors without optimization, and dashed lines - with optimization; red color corresponds to displacement along the x-axis, green to the y-axis, blue to the z-axis. The x-axis is directed from the stationary camera towards the moving camera, the z-axis is oriented in the direction of the measurement object, respectively, the y-axis is perpendicular to the x-axis and z-axis and is directed downward, i.e. towards the base of the camera tripod. The measurements were carried out for various shapes of the object surface (a, b and c on Figure 3 respectively). The offset steps for all axes to either side of zero are 1, 5, and 10 mm in positioner coordinates. The position on the positioner x = 25 mm, y = 25 mm and z = 25 mm is taken as the offset zero. the positioner offset range is 50 mm.

From the data obtained, we can conclude that for all three surface shapes, the same dependence of the reprojection error is visible without optimization for the x, y, and z axes. The offset along the y-axis is most influential, slightly less along the x-axis, and displacement along the z-axis has little effect on the error.

Thanks to optimization for the first shape of the object surface, it was possible to reduce the error at all camera positions to values less than 0.1 pixels, for the second shape, less than 4.0 pixels, and for the third shape, less than 0.25 pixels. Although for the second shape of the object's surface, the minimum error is clearly not achieved, its decrease is significant at displacements of 5 and 10 mm. For the first and third shapes of the object's surface, it turned out to fall below the calibration values of the error and to maintain errors close to these values even at displacements of 5 and 10 mm.

In the above results, as in computer modeling, the Nelder-Mead optimization method was used in conjunction with the penalty function method, where the restrictions on the search for displacements relative to the beginning of the search are  $\pm 10$  mm, and the rotation is  $\pm 2^{\circ}$ . With the maximum number of iterations in one attempt 500 and the number of attempts equal to 12. The optimization used all the points in the image, which was obtained as a result of cross-correlation.

From Figure 3, we can conclude that the implemented algorithm successfully copes with reducing the reprojection error. We also note that if there is a need to speed up the operation of the algorithm, then you can use not all image points for optimization and try to reduce the number of attempts to find a solution.

## 4. Conclusion

The paper shows one of the approaches to optimizing the reprojection error function to find the actual parameters of the stereo system calibration. Actual parameters may change during measurements under high vibration loads, and this leads to increased measurement error. The reprojection error function is optimized with the Nelder-Mead algorithm for a function of six variables: displacement amplitudes and angles of rotation along three axes. It is impossible to determine the accuracy characteristic of the algorithm directly since it depends on many factors, but it is possible to estimate the achieved values of the objective function as a result of optimization. As a result of the optimization, the values of the reprojection error likely are the same as at the calibration stage and even smaller values.

In the work, a computer and physical modeling of the decalibration process in laboratory conditions was carried out with the subsequent application of the recalibration procedure. In the course of the latter, the reprojection error has decreased significantly. However, it cannot be said unequivocally that recalibration allows one to determine the ongoing changes in the position of the cameras. Further

research will be aimed at increasing the number of experiments carried out for the collection of statistics and comparing the optimized calibration parameters with those specified in the modeling.

#### 5. Acknowledgements

The investigation was carried out within the framework of the project "Development of photogrammetric surface shape measurement system for the conditions of high vibration loads" with the support of a grant from NRU "MPEI" for implementation of scientific research programs "Energy", "Electronics, Radio Engineering and IT", and "Industry 4.0, Technologies for Industry and Robotics" in 2020–2022.

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