



# SWiM – A Semantic Wiki for Mathematical Knowledge Management

SWiM is a semantic wiki for collaboratively building, editing, browsing, and discussing collections of mathematical knowledge represented in structural semantic markup. It motivates users to contribute by instantly sharing the benefits of knowledge-powered services with them.

## User

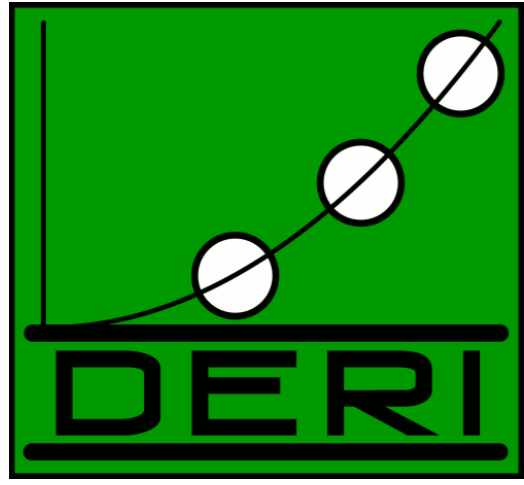
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## Search

$\int_?^? s^2(t)dt$

Go!

## Import

- OpenMath CD
- OMDoc
- Ontology
- $\LaTeX$

## Export

- OpenMath CD
- OMDoc
- XHTML+MathML
- RDF
- PDF

## Mathematical Knowledge Management

Goal: web collaboration on structured mathematical knowledge

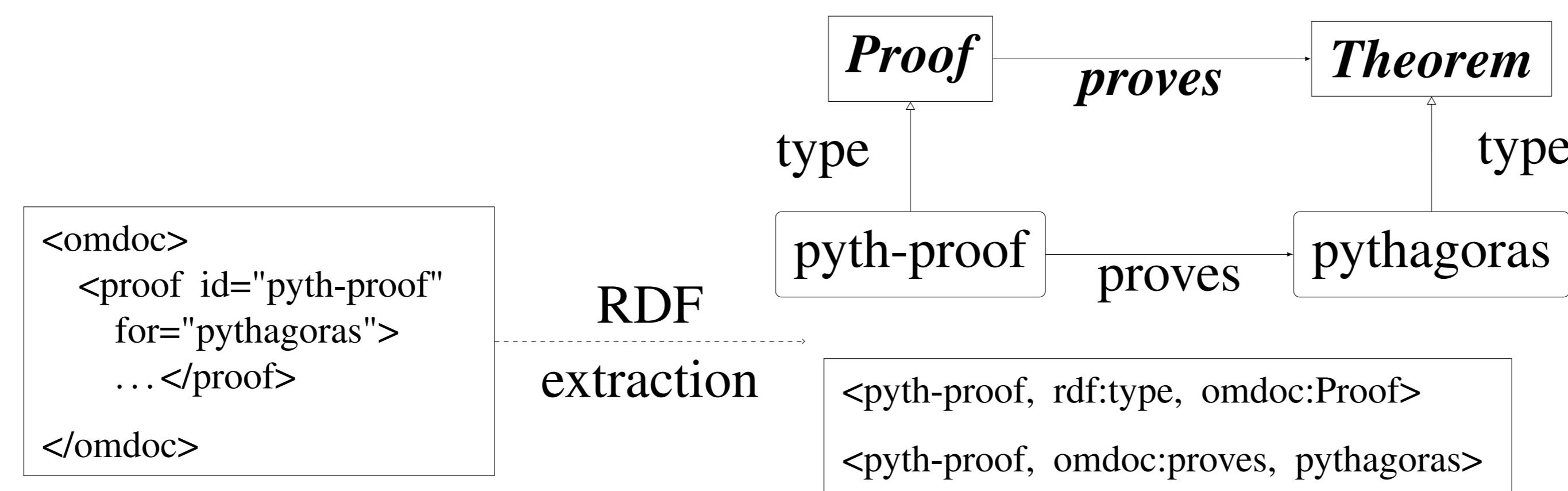
- semantic markup common for documents in mathematics: MathML, OpenMath, OMDoc,  $\LaTeX$
- layers of knowledge: symbols, statements, theories, documents
- applications: e-learning, publishing, proof verification
- but how to acquire the knowledge?
- $\Rightarrow$  services to motivate the user and support the authoring workflow

```
<apply>
  <csymbol definitionURL=
    "http://openmath.org/cd/
    arith1#plus"/>
  <cn type="integer">1</cn>
  <ci>n</ci>
</apply>
```

A "simple" semantic formula

## Semantic Wiki and Ontologies

- Semantic wikis found usable to support collaborative formalisation
- Difference here is: deeply nested markup, lots of cross-references
- Right granularity of pages: one page = one theory, one statement, one formula?
- $\Rightarrow$  extract knowledge relevant for search and navigation, build most services on top of that
- RDF graph in terms of an ontology that models the semantics of the markup; direct and inferred relationships: dependency, containment



$$\text{SWiM} = \text{IkeWiki} + \text{OMDoc} + \sum_{i=1}^{\infty} \sigma_i, \sigma_i \in \text{service}$$

Technical foundations:

- IkeWiki [Schaffert]
- OMDoc [Kohlhase]

Features:

- editing
- presentation
- navigation
- discourse
- import/export
- refactoring
- semantic services

## OpenMath 3 Case Study

- revision of the content dictionaries (collections of symbol definitions)
- user interface: editing formulae, metadata, symbol notations

Examples for notational preferences:

- language:  $\binom{n}{k}, C_n^k, C_k^n$
- domain:  $\sqrt{-1} = i, \sqrt{-1} = j$
- taste:  $f'''(x), f^{(2)}(x), \frac{d^2y}{dx^2}, \frac{d^2}{dx^2}f(x)$
- exactness:  $f \in \mathcal{O}(n), f = \mathcal{O}(n)$

## Flyspeck Case Study

- Formalising a Proof of the Kepler conjecture [Hales 1998]
- hundreds of proof sketches (400 pages  $\LaTeX$ ), collaboratively transform them into something machine-verifiable
- formalising, annotating, discussing, project management



## References

- hasDemo  
http://swim.kwarc.info
- homepageURL  
http://kwarc.info/projects/swim/
- presentedAt  
Semantic Wiki Workshop  
JEM Workshop (Joining Educational Mathematics)  
MathUI Workshop
- rdfs:seeAlso  
PlanetMath  
Semantic MediaWiki  
Connexions  
ActiveMath
- rdf:type  
Semantic Wiki  
Mathematical Editor  
Collaboration Tool  
Browser

## Conclusion

- SWiM makes mathematical documents editable collaboratively and facilitates common workflows by exploiting the knowledge they contain.
- Domain-specific markup and ontology allows for advantages over generic semantic wikis and non-semantic mathematical wikis w.r.t. knowledge management
- Approach transferable to other domains (e.g. chemistry): decide on page granularity, capture semantics in ontology, extract RDF, integrate suitable editors

## Roadmap

- ontology for narrative structures
- formalisation workflow
- dependency graph navigation
- refactoring support
- adaptive presentation

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