

# Keyword Search in the Deep Web

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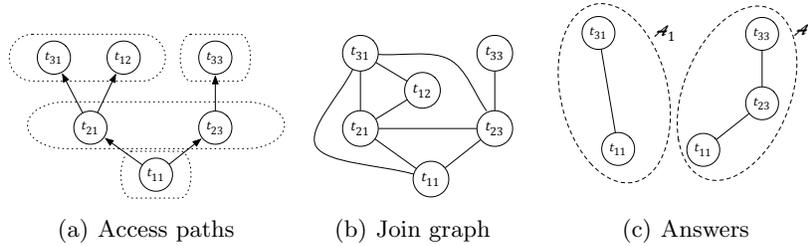
**Abstract.** The Deep Web is constituted by data accessible through Web pages, but not readily indexable by search engines, as they are returned in dynamic pages. In this paper we propose a framework for accessing Deep Web sources, represented as relational tables with so-called access limitations, with keyword-based queries. We formalize the notion of optimal answer and investigate methods for query processing. To our knowledge, this problem has never been studied in a systematic way.

## 1 Problem definition

*Basics.* We model data sources as relations of a relational database and we assume that, albeit autonomous, they have “compatible” attributes. For this, we assume that the attributes of relations are defined over a set of *abstract domains*  $\mathbf{D} = \{D_1, \dots, D_m\}$ , which, rather than denoting concrete value types (such as string or integer), represent data types at a higher level of abstraction (for instance, *car* or *country*). The set of all values is denoted by  $\mathcal{D} = \bigcup_{i=1}^m D_i$ .

In the following, we shall denote by  $R(A_1, \dots, A_k)$  a (relation) schema, by  $\text{dom}(A) \in \mathbf{D}$  the domain of an attribute  $A$ , by  $r$  a relation over  $R$ , and by  $\mathbf{r} = \{r_1, \dots, r_n\}$  a (database) instance of a database schema  $\mathbf{R} = \{R_1, \dots, R_n\}$ .

*Access limitations.* An *access pattern*  $\Pi$  for a schema  $R(A_1, \dots, A_k)$  is a mapping sending each attribute  $A_i$  into an *access mode*, which can be either input or output;  $A_i$  is correspondingly called an *input* (resp., *output*) *attribute* for  $R$  wrt.  $\Pi$ . For ease of notation, we shall mark input attributes with an ‘ $i$ ’ superscript to distinguish them from the output ones. Let  $A'_1, \dots, A'_l$  be all the input attributes for  $R$  wrt.  $\Pi$ ; any tuple  $\langle c_1, \dots, c_l \rangle$  such that  $c_i \in \text{dom}(A'_i)$  for  $1 \leq i \leq l$  is called a *binding* for  $R$  wrt.  $\Pi$ . An *access*  $\alpha$  consists of an access pattern  $\Pi$  for a schema  $R$  and a binding for  $R$  wrt.  $\Pi$ ; the *output* of such an access  $\alpha$  on an instance  $\mathbf{r}$  is the set  $\mathcal{T} = \sigma_{A_1=c_1, \dots, A_l=c_l}(r)$ . Intuitively, we can only access a relation if we can provide a value for every input attribute. Given an instance  $\mathbf{r}$  for a database schema  $\mathbf{R}$ , a set of access patterns  $\mathbf{\Pi}$  for the relations in  $\mathbf{R}$ , and a set of values  $\mathcal{C} \subseteq \mathcal{D}$ , an *access path* (for  $\mathbf{R}$ ,  $\mathbf{\Pi}$  and  $\mathcal{C}$ ) is a sequence of accesses  $\alpha_1, \dots, \alpha_n$  on  $\mathbf{r}$  such that each value in the binding of  $\alpha_i$ ,  $1 \leq i \leq n$ , either occurs in the output of an access  $\alpha_j$  with  $j < i$  or is a value in  $\mathcal{C}$ . A tuple  $t$  in  $\mathbf{r}$  is said to be *reachable* if there exists an access path  $P$  such that  $t$  is in the output of some



**Fig. 1.** Example 1: Reachable portion, corresponding join graph, and answers.

access in  $P$ ; the *reachable portion*  $\text{reach}(\mathbf{r}, \mathbf{II}, \mathcal{C})$  of  $\mathbf{r}$  is the set of all reachable tuples in  $\mathbf{r}$  given the values in  $\mathcal{C}$ .

*Keyword queries.* A keyword query is a set of values in  $\mathcal{D}$  called *keywords*.

**Example 1** Consider a query  $q = \{k_1, k_2\}$ , a schema (with access patterns  $\mathbf{II}$ )  $\mathbf{R} = \{R_1(A_1^i, A_2), R_2(A_2^i, A_1), R_3(A_1^i, A_2, A_3)\}$ , and an instance  $\mathbf{r}$  such that

$$r_1 = \begin{array}{|c|c|} \hline A_1^i & A_2 \\ \hline k_1 & c_1 \\ \hline c_2 & c_3 \\ \hline \end{array} t_{11} \quad r_2 = \begin{array}{|c|c|} \hline A_2^i & A_1 \\ \hline c_1 & c_2 \\ \hline c_4 & c_2 \\ \hline c_1 & c_6 \\ \hline \end{array} t_{21} \quad r_3 = \begin{array}{|c|c|c|} \hline A_1^i & A_2 & A_3 \\ \hline c_2 & c_1 & k_2 \\ \hline c_5 & c_4 & k_2 \\ \hline c_6 & c_7 & k_2 \\ \hline \end{array} \begin{array}{l} t_{31} \\ t_{32} \\ t_{33} \end{array}$$

Figure 1(a) shows the reachable portion of  $\mathbf{r}$  given the values in  $q$  along with the access paths used to extract it, with dotted lines enclosing outputs of accesses. ■

Given a set  $\mathcal{T}$  of tuples, the *join graph* of  $\mathcal{T}$  is a node-labelled undirected graph  $\mathcal{T} = \langle N, E \rangle$  constructed as follows: (i) the nodes  $N$  are labelled with tuples of  $\mathcal{T}$ , and (ii) there is an arc between two nodes  $n_1$  and  $n_2$  if the tuples labelling  $n_1$  and  $n_2$  have at least one value in common.

**Example 1 (cont.)** The join graph of  $\text{reach}(\mathbf{r}, \mathbf{II}, q)$  is shown in Figure 1(b).

■  
**Definition 1 (Answer).** An answer to a keyword query  $q$  against a database instance  $\mathbf{r}$  over a schema  $\mathbf{R}$  with access patterns  $\mathbf{II}$  is a set of tuples  $\mathcal{A}$  in  $\text{reach}(\mathbf{r}, \mathbf{II}, q)$  such that: (1) each  $c \in q$  occurs in at least one tuple  $t$  in  $\mathcal{A}$ ; (2) the join graph of  $\mathcal{A}$  is connected; (3) for every subset  $\mathcal{A}' \subseteq \mathcal{A}$  such that  $\mathcal{A}'$  enjoys Condition 1 above, the join graph of  $\mathcal{A}'$  is not connected.

It is straightforward to see that there could be several answers to a keyword query; below we give a widely accepted criterium for ranking such answers [4].

**Definition 2.** Let  $\mathcal{A}_1, \mathcal{A}_2$  be two answers of a keyword query  $q$  on an instance  $\mathbf{r}$  of size  $|\mathcal{A}_1|$  and  $|\mathcal{A}_2|$  respectively; we say that  $\mathcal{A}_1$  is better than  $\mathcal{A}_2$ , denoted  $\mathcal{A}_1 \preceq \mathcal{A}_2$ , if  $|\mathcal{A}_1| \leq |\mathcal{A}_2|$ . The optimal answers are those of minimum size.

**Example 1 (cont.)** The sets  $\mathcal{A}_1 = \{t_{11}, t_{31}\}$  and  $\mathcal{A}_2 = \{t_{11}, t_{23}, t_{33}\}$  are answers to  $q$ ;  $\mathcal{A}_1$  is better than  $\mathcal{A}_2$  and is the optimal answer to  $q$ . ■

## 2 Keyword-based answering in the Deep Web

We now present a vanilla algorithm to discuss the computational complexity of answering a keyword query  $q$  in the deep Web modeled as an instance  $\mathbf{r}$  of a schema  $\mathbf{R}$  with access patterns  $\mathbf{II}$ . Example 1 shows that, in the worst case, we need to extract the whole reachable portion to obtain the tuples involved in an optimal answer. In fact,  $\mathbf{s} = reach(\mathbf{r}, \mathbf{II}, q)$  is actually a connected join graph, since every tuple in it is in some output of some access path starting from the values in the query (see for example Figure 1.a), but further paths may exist between tuples in  $\mathbf{s}$  (see Figure 1.b). Therefore, query answering requires in general two main steps, described in Algorithm 1: (i) extract the reachable portion  $\mathbf{s}$  of  $\mathbf{r}$ ; (ii) if possible, remove tuples from  $\mathbf{s}$  so that the obtained set satisfies the conditions of Definition 1, while minimizing its size.

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### Algorithm 1: Computing an optimal answer ( $Answer(q, \mathbf{II}, \mathbf{r})$ )

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Input: Keyword query  $q$ , access patterns  $\mathbf{II}$ , instance  $\mathbf{r}$  over  $\mathbf{R}$

Output: Answer  $\mathcal{A}$

1.  $\mathcal{A} := reachablePortion(\mathbf{r}, \mathbf{II}, q)$ ; // see Algorithm 2
  2. if  $\mathcal{A}$  does not contain all values in  $q$  then return nil;
  3. else  $prune(\mathcal{A}, q)$ ; // see Algorithm 3
  4. return  $\mathcal{A}$ ;
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A simple way of extracting the reachable portion, inspired by the procedure described in [1], is shown in Algorithm 2. This algorithm may be allowed to terminate early if the answer is not required to be optimal (flag  $\omega$  set to *false*), and thus can stop as soon as the reachable portion contains all the keywords in the query. This is coherent with the *distinct root-based semantics* of keyword search in relational databases, which provides a tradeoff between quality of the result and efficiency of the method to evaluate it [4].

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### Algorithm 2: Reachable portion ( $reachablePortion(\mathbf{r}, \mathbf{II}, q)$ )

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Input: Instance  $\mathbf{r}$  over  $\mathbf{R}$ , access patterns  $\mathbf{II}$ , initial values  $q$

Flag: boolean  $\omega$  // if  $\omega = true$  the answer is guaranteed to be optimal

Output: Reachable portion  $RP$

1.  $RP := \emptyset$ ;  $\mathcal{C} := \emptyset$ ;
  2. while an access can be made with a new binding  $b$  for some  $R \in \mathbf{R}$  wrt.  $\mathbf{II}$  using values in  $\mathcal{C} \cup q$
  3.    $\mathcal{O} :=$  output of access to  $r$  over  $R$  with binding  $b$ ;
  4.    $RP := RP \cup \mathcal{O}$ ; // cumulating all the obtained tuples into  $RP$
  5.    $\mathcal{C} := \mathcal{C} \cup \bigcup_{A \in R, t \in \mathcal{O}} \{t(A)\}$ ; // cumulating all the obtained values into  $\mathcal{C}$
  6.   if  $\mathcal{C} \supseteq q \wedge \neg \omega$  then break;
  7. return  $RP$ ;
- 

Basically, determining an optimal answer from the reachable portion corresponds to finding a Steiner tree of its join graph [4], i.e., a minimal-weight subtree of this graph involving a subset of its nodes. An efficient method for solving this problem in the context of keyword search over structured data is presented in [2], where a *q-fragment* can model our notion of answer. Yet, when optimality is not required, a simple technique (quadratic in the size of  $\mathbf{r}$ ) to obtain an answer (steps 2–6 of Algorithm 3) consists in trying to remove any tuple from the set as long as it contains all the keywords and remains connected.

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**Algorithm 3:** Pruning ( $prune(\mathcal{T}, q)$ )

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Input: Set of tuples  $\mathcal{T}$ , keyword query  $q$

Flag: boolean  $\omega$  // if  $\omega = true$  the answer is guaranteed to be optimal

Output: Minimal set of tuples  $\mathcal{T}$

1. **if**  $\omega$  **then return** a minimal subtree of the join graph of  $\mathcal{T}$  that contains  $q$ ;
  2.  $\mathcal{T}' := \mathcal{T}$ ;  $\mathcal{T}'' := \emptyset$ ;
  3. **while**  $\mathcal{T}'' \neq \mathcal{T}'$
  4.      $\mathcal{T}'' := \mathcal{T}'$ ;
  5.     **for each**  $t \in \mathcal{T}''$  **if**  $\mathcal{T}' \setminus \{t\}$  is connected and  $\mathcal{T}' \setminus \{t\} \supseteq q$  **then**  $\mathcal{T}' := \mathcal{T}' \setminus \{t\}$ ;
  6. **return**  $\mathcal{T}'$ ;
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The extraction of the reachable portion of an instance  $\mathbf{r}$  with access limitations can be implemented by a Datalog program over  $\mathbf{r}$  [1], which can be evaluated in polynomial time in the size of the input [3]. In addition, in [2] it is shown that the optimal  $q$ -fragments of  $\mathbf{r}$  can be enumerated in ranked-order with polynomial delay, i.e., the time for printing the next optimal answer is again polynomial in the size of  $\mathbf{r}$ . Hence, we can state the following preliminary result.

**Theorem 1.** *An optimal answer to a keyword query against a database instance with access limitations can be efficiently computed under data complexity.*

### 3 Discussion and future work

In this paper, we have defined the problem of keyword search in the Deep Web and provided some preliminary insights on query answering in this context. As future work on the problem in question, we plan to:

- devise optimization strategies for query answering; in particular, identify conditions under which an optimal answer can be derived without extracting the whole reachable instance;
- leverage known values (besides the keywords), modeled as relations with only one (output) attribute, to speed up the search for an optimal answer;
- study the problem in a scenario in which the domains of the keywords are known in advance: in this case schema-based techniques can be used;
- consider the case in which nodes and arcs of the join graph are weighted to model source availability and proximity, respectively.

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