















data cube, the operators CUBE and ROLLUP are implemented. If necessary, in data integrated schemas new super-aggregate operators can be define. We use a computationally complete language to create schemas of integrated data. Applying the query language to the integrated data is generated a reduction problem. Supporting the query language over such data requires additional investigations.

Finally, modern trends of the development of database systems lead to the application of different divisions of mathematics to data analysis and management. In the frame of our approach to data integration, this leads to the use of corresponding content dictionaries of the OPENMath.

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